Welcome

2020 will go down in history. The world has changed for all of us.

We want to do as much as we can to support children, teachers, parents and carers in these very uncertain times.

We have amended our schemes for 2020/21 to:

★ highlight key teaching points
★ recap essential content that children may have forgotten
★ flag any content that you might not have covered during the school closures period.

We hope these changes will add further value to the schemes and save you time.

Lesson-by-lesson overviews

We’ve always been reluctant to produce lesson-by-lesson overviews as every class is individual and has different needs. However, many of you have said that if blended learning becomes a key feature of school life next year, a weekly plan with linked content and videos could be really useful.

As always, we’ve listened! We’ve now produced a complete lesson-by-lesson overview for Y1 to Y9 that schools can use or adapt as they choose. Each lesson will be linked to a free-to-use home learning video, and for premium subscribers, a worksheet. This means that you can easily assign work to your class, whether they are working at home or in school.

Inevitably, this lesson-by-lesson structure won’t suit everyone, but if it works for you, then please do make use of this resource as much as you wish.
Teaching for Mastery

These overviews are designed to support a mastery approach to teaching and learning and have been designed to support the aims and objectives of the new National Curriculum.

The overviews:

• have number at their heart. A large proportion of time is spent reinforcing number to build competency
• ensure teachers stay in the required key stage and support the ideal of depth before breadth.
• ensure students have the opportunity to stay together as they work through the schemes as a whole group
• provide plenty of opportunities to build reasoning and problem solving elements into the curriculum.

For more guidance on teaching for mastery, visit the NCETM website:
https://www.ncetm.org.uk/resources/47230

Concrete - Pictorial - Abstract

We believe that all children, when introduced to a new concept, should have the opportunity to build competency by taking this approach.

Concrete – children should have the opportunity to use concrete objects and manipulatives to help them understand what they are doing.

Pictorial – alongside this children should use pictorial representations. These representations can then be used to help reason and solve problems.

Abstract – both concrete and pictorial representations should support children’s understanding of abstract methods.

Need some CPD to develop this approach? Visit www.whiterosemaths.com for find a course right for you.
Supporting resources

We have produced supporting resources for every small step from Year 1 to Year 11.

The worksheets are provided in three different formats:

- **Write on worksheet** – ideal for children to use the ready made models, images and stem sentences.
- **Display version** – great for schools who want to cut down on photocopying.
- **PowerPoint version** – one question per slide. Perfect for whole class teaching or mixing questions to make your own bespoke lesson.

For more information visit our online training and resources centre [resources.whiterosemaths.com](http://resources.whiterosemaths.com) or email us directly at [support@whiterosemaths.com](mailto:support@whiterosemaths.com)
Meet the Characters

Children love to learn with characters and our team within the scheme will be sure to get them talking and reasoning about mathematical concepts and ideas. Who’s your favourite?
<table>
<thead>
<tr>
<th>Week</th>
<th>Autumn</th>
<th>Spring</th>
<th>Summer</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Number: Place Value</td>
<td>Number: Decimals</td>
<td>Geometry: Properties of Shape</td>
</tr>
<tr>
<td>2</td>
<td>Number: Addition, Subtraction, Multiplication and Division</td>
<td>Number: Percentages</td>
<td>Consolidation or SATs preparation</td>
</tr>
<tr>
<td>3</td>
<td>Number: Fractions</td>
<td>Number: Algebra</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>Geometry: Position and Direction</td>
<td>Measurement: Converting Units</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>Measurement: Perimeter, Area and Volume</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td></td>
<td></td>
<td>Consolidation, investigations and preparations for KS3</td>
</tr>
<tr>
<td>7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>9</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>12</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Overview
Small Steps

- Decimals up to 2 decimal places
- Understand thousandths
- Three decimal places
- Multiply by 10, 100 and 1,000
- Divide by 10, 100 and 1,000
- Multiply decimals by integers
- Divide decimals by integers
- Division to solve problems
- Decimals as fractions
- Fractions to decimals (1)
- Fractions to decimals (2)

Notes for 2020/21

The recap steps are at the beginning of this block to ensure children have a good understanding of numbers up to three decimal places before moving on to multiplication and division.

This should build on place value work in the autumn term and make use of place value grids and counters to build on previous learning.
Children use place value counters and a place value grid to make numbers with up to two decimal places.

They read and write decimal numbers and understand the value of each digit.

They show their understanding of place value by partitioning decimal numbers in different ways.

### Notes and Guidance

**Mathematical Talk**

- How many ones/tenths/hundredths are in the number?
- How do we write this as a decimal? Why?
- What is the value of the ____ in the number ______?
- When do we need to use zero as a place holder?
- How can we partition decimal numbers in different ways?

### Varied Fluency

#### Which number is represented on the place value chart?

<table>
<thead>
<tr>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

There are ____ ones, ____ tenths and ____ hundredths.

The number is ____

#### Represent the numbers on a place value chart and complete the stem sentences.

<table>
<thead>
<tr>
<th>Number</th>
<th>0.28</th>
<th>0.65</th>
<th>0.07</th>
<th>1.26</th>
</tr>
</thead>
</table>

#### Make the numbers with place value counters and write down the value of the underlined digit.

<table>
<thead>
<tr>
<th>Number</th>
<th>2.45</th>
<th>3.04</th>
<th>4.44</th>
<th>43.34</th>
</tr>
</thead>
</table>

0.76 = 0.7 + 0.06 = 7 tenths and 6 hundredths.

Fill in the missing numbers.

0.83 = ____ + 0.03 = ___________ and 3 hundredths.

0.83 = 0.7 + ____ = 7 tenths and ___________

How many other ways can you partition 0.83?
Dexter says there is only one way to partition 0.62

Prove Dexter is incorrect by finding at least three different ways of partitioning 0.62

0.62 = 0.12 + 0.5
0.62 = 0.4 + 0.22
0.62 = 0.3 + 0.32
0.62 = 0.42 + 0.2
0.62 = 0.1 + 0.52
0.62 = 0.03 + 0.59

etc.

Match each description to the correct number.

Teddy – 40.46
Amir – 46.2
Rosie – 46.02
Eva – 2.64

Teddy – My number has the same amount of tens and tenths.
Amir – My number has one decimal place.
Rosie – My number has two hundredths.
Eva – My number has six tenths.
Understanding Thousandths

Notes and Guidance

Children build on previous learning of tenths and hundredths and apply this to understanding thousandths. Opportunities to develop understanding of thousandths through the use of concrete and pictorial representations need to be incorporated. When exploring the relationships between tenths, hundredths and thousandths, consider decimal and mixed number equivalences.

Mathematical Talk

If 4 tenths = 0.4, 4 hundredths = 0.04, what is 4 thousandths equal to?

Using the place value charts:
- How many tenths are in a whole?
- How many hundredths are there in 1 tenth?
- Using place value counters complete the final chart.
- How many thousandths in 1 hundredth?

Varied Fluency

Eva is using Base 10 to represent decimals.

\[\begin{align*}
\text{= } & \quad \text{1 whole} \\
\text{= } & \quad \text{1 tenth} \\
\text{= } & \quad \text{1 hundredth} \\
\text{= } & \quad \text{1 thousandth}
\end{align*}\]

Use Base 10 to build:
- 4 wholes, 4 tenths, 4 hundredths, 4 thousandths
- 5 tenths, 7 hundredths and 5 thousandths
- 2.357

Use the place value counters to help you fill in the final chart.

What has this hundred square been divided up into?
How many thousandths are there in one hundredth?
How many thousandths are in one tenth?
Rosie thinks the 2 values are equal.

Agree.

We can exchange ten hundredth counters for one tenth counter.

$$0.135 = \frac{135}{1000}$$

Do you agree?
Explain your thinking.

Can you write this amount as a decimal and as a fraction?

0.394

= 3 tenths, 9 hundredths and 4 thousandths

$$= \frac{3}{10} + \frac{9}{100} + \frac{4}{1000}$$

= 0.3 + 0.09 + 0.004

Write these numbers in three different ways:

0.472 = 4 tenths, seven hundredths and 2 thousandths

$$= \frac{4}{10} + \frac{7}{100} + \frac{2}{1000}$$

= 0.4 + 0.07 + 0.002

0.529 = 5 tenths, two hundredths and 9 thousandths

$$= \frac{5}{10} + \frac{2}{100} + \frac{9}{1000}$$

= 0.5 + 0.02 + 0.009

0.307 = 3 tenths and 7 thousandths

$$= \frac{3}{10} + \frac{7}{1000}$$

= 0.3 + 0.007
Three Decimal Places

Notes and Guidance

Children recap their understanding of numbers with up to 3 decimal places. They look at the value of each place value column and describe its value in words and digits.

Children use concrete resources to investigate exchanging between columns e.g. 3 tenths is the same as 30 hundredths.

Mathematical Talk

How many tenths are there in the number? How many hundredths? How many thousandths?

Can you make the number on the place value chart?

How many hundredths are the same as 5 tenths?

What is the value of the zero in this number?

Varied Fluency

Complete the sentences.

There are ____ ones, ____ tenths, ____ hundredths and ____ thousandths.
The number in digits is ______________

Use counters and a place value chart to represent these numbers.

<table>
<thead>
<tr>
<th></th>
<th>0.001</th>
<th>0.001</th>
<th>0.001</th>
<th>0.001</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>0.1</td>
<td>0.1</td>
<td></td>
</tr>
</tbody>
</table>

Write down the value of the 3 in the following numbers.

0.53  362.44  739.8  0.013  3,420.98
Reasoning and Problem Solving

Tommy says,

The more decimal places a number has, the smaller the number is.

Do you agree? Explain why.

Alex says that 3.24 can be written as 2 ones, 13 tenths and 4 hundredths.

Do you agree?

How can you partition 3.24 starting with 2 ones?
How can you partition 3.24 starting with 1 one?
Think about exchanging between columns.

Possible answer:

I do not agree with this as the number 4.39 is smaller than the number 4.465, which has more decimal places.

Possible answer:

I disagree; Alex’s numbers would total 3.34. I could make 3.24 by having 2 ones, 12 tenths and 4 hundredths or 1 one, 22 tenths and 4 hundredths.

Four children are thinking of four different numbers.

Teddy: 4.345
Alex: 4.445
Dora: 3.454
Jack: 3.54

Teddy: “My number has four hundredths.”

Alex: “My number has the same amount of ones, tenths and hundredths.”

Dora: “My number has less ones that tenths and hundredths.”

Jack: “My number has 2 decimal places.”

Match each number to the correct child.
Notes and Guidance

Children multiply numbers with up to three decimal places by 10, 100 and 1,000. They discover that digits move to the left when they are multiplying and use zero as a place value holder. The decimal point does not move. Once children are confident in multiplying by 10, 100 and 1,000, they use these skills to investigate multiplying by multiples of these numbers, e.g., $2.4 \times 20$.

Mathematical Talk

What number is represented on the place value chart?

Why is 0 important when multiplying by 10, 100 and 1,000?

What patterns do you notice?

What is the same and what is different when multiplying by 10, 100, 1,000 on the place value chart compared with the Gattegno chart?

Varied Fluency

Identify the number represented on the place value chart.

<table>
<thead>
<tr>
<th>Thousands</th>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>0</td>
</tr>
</tbody>
</table>

Multiply it by 10, 100, and 1,000 and complete the sentence stem for each.

When multiplied by ____ the counters move ____ places to the _____.

Use a place value chart to multiply the following decimals by 10, 100, and 1,000.

- $6.4 \times 20 = 128$
- $6.04 \times 100 = 604$
- $6.004 \times 1,000 = 6,004$

Fill in the missing numbers in these calculations:

- $32.4 \times \_ \_ \_ = 324$
- $1.562 \times 1,000 = \_ \_ \_ \_ \_ $
- $\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \times 100 = 208$
- $4.3 \times \_ \_ \_ \_ \_ = 86$
Using the digit cards 0-9 create a number with up to 3 decimal places e.g. 3.451
Cover the number using counters on your Gattegno chart.

Children will be able to see how the counter will move up a row for multiplying by 10, two rows for 100 and three rows for 1,000. They can see that this happens to each digit regardless of the value. For example, 3.451 \times 10 \text{ becomes } 34.51
Each counter moves up a row but stays in the same column.

When you multiply by 100, you should add two zeros.

Dora says,
Do you agree?
Explain your thinking.

Children should explain that when you multiply by 100 the digits move two places to the left.
For example: 0.34 \times 100 = 0.3400 is incorrect as 0.34 is the same as 0.3400
Also: 0.34 + 0 + 0 = 0.34
Children show 0.34 \times 100 = 34
Divide by 10, 100 and 1,000

Notes and Guidance

Once children understand how to multiply decimals by 10, 100 and 1,000, they can apply this knowledge to division, which leads to converting between units of measure.

It is important that children continue to understand the importance of 0 as a place holder. Children also need to be aware that 2.4 and 2.40 are the same. Similarly, 12 and 12.0 are equivalent.

Mathematical Talk

What happens to the counters/digits when you divide by 10, 100 or 1,000?

Why is zero important when dividing by 10, 100 and 1,000?

What is happening to the value of the digit each time it moves one column to the right?

What are the relationships between tenths, hundredths and thousandths?

Varied Fluency

Use the place value chart to divide the following numbers by 10, 100 and 1,000

<table>
<thead>
<tr>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
<th>Thousandths</th>
</tr>
</thead>
<tbody>
<tr>
<td>44</td>
<td>1.36</td>
<td>107</td>
<td>5</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Tick the correct answers. Can you explain the mistakes with the incorrect answers?

Complete the table.

<table>
<thead>
<tr>
<th>±10</th>
<th>±100</th>
<th>±1000</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3 kg</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.9</td>
<td></td>
<td>9.0</td>
</tr>
<tr>
<td>9.09</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Using the following rules, how many ways can you make 70?

- Use a number from column A
- Use an operation from column B.
- Use number from column C.

Possible answers:

- $0.7 \times 100$
- $7 \times 10$
- $70 \div 10$
- $700 \div 100$
- $70 \div 1$

Eva says,

When you divide by 10, 100 or 1,000 you just take away the zeros or move the decimal point.

Eva is wrong, the decimal point never moves. When dividing, the digits move right along the place value columns.

Possible examples to prove Eva wrong:

- $24 \div 10 = 2.4$
- $107 \div 10 = 17$

This shows that you cannot just remove a zero from the number.
Mathematical Talk

Which is bigger, 0.1, 0.01 or 0.001? Why?

How many 0.1s do you need to exchange for a whole one?

Can you draw a bar model to represent the problem?

Can you think of another way to multiply by 5? (e.g. multiply by 10 and divide by 2).

Notes and Guidance

Children use concrete resources to multiply decimals and explore what happens when you exchange with decimals.

Children use their skills in context and make links to money and measures.

Varied Fluency

Use the place value counters to multiply 1.212 by 3
Complete the calculation alongside the concrete representation.

<table>
<thead>
<tr>
<th>Tens</th>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
<th>Thousandths</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.1</td>
<td>0.01</td>
<td>0.001</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>0.1</td>
<td>0.01</td>
<td>0.001</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>0.1</td>
<td>0.01</td>
<td>0.001</td>
<td></td>
</tr>
</tbody>
</table>

A jar of sweets weighs 1.213 kg.
How much would 4 jars weigh?

Rosie is saving her pocket money. Her mum says,

“Whatever you save, I will give you five times the amount.”

If Rosie saves £2.23, how much will her mum give her?
If Rosie saves £7.76, how much will her mum give her? How much will she have altogether?
Reasoning and Problem Solving

Whitney says, "Do you agree? Explain why."

Possible answer: I do not agree because there are examples such as $2.23 \times 2$ that gives an answer with only two decimal places.

Chocolate eggs can be bought in packs of 1, 6 or 8. What is the cheapest way for Dexter to buy 25 chocolate eggs?

He should buy four packs of 6 plus an individual egg.

<table>
<thead>
<tr>
<th>Fill in the blanks</th>
<th>Multiply Decimals by Integers</th>
</tr>
</thead>
<tbody>
<tr>
<td>$3 \cdot 4 \cdot 5$</td>
<td>$3 \cdot 4 \cdot 5$</td>
</tr>
<tr>
<td>$0 \cdot 3 \cdot 0$</td>
<td>$0 \cdot 3 \cdot 0$</td>
</tr>
<tr>
<td>$1 \cdot 0 \cdot 0$</td>
<td>$1 \cdot 0 \cdot 0$</td>
</tr>
<tr>
<td>$1 \cdot 8 \cdot 0 \cdot 0$</td>
<td>$2 \cdot 4 \cdot 0$</td>
</tr>
<tr>
<td>$2 \cdot 0 \cdot 7 \cdot 0$</td>
<td>$6$</td>
</tr>
</tbody>
</table>

| 1 chocolate egg | £0.52 |
| 6 chocolate eggs | £2.85 |
| 8 chocolate eggs | £4.00 |

| £11.92 |
| Dexter should buy four packs of 6 plus an individual egg. |
Divide Decimals by Integers

Notes and Guidance

Children continue to use concrete resources to divide decimals and explore what happens when exchanges take place.

Children build on their prior knowledge of sharing and grouping when dividing and apply this skill in context.

Mathematical Talk

Are we grouping or sharing?

How else could we partition the number 3.69? (For example, 2 ones, 16 tenths and 9 hundredths.)

How could we check that our answer is correct?

Varied Fluency

Divide 3.69 by 3

Use the diagrams to show the difference between grouping and by sharing?

Use these methods to complete the sentences.

3 ones divided by 3 is __________ ones.

6 tenths divided by 3 is __________ tenths.

9 hundredths divided by 3 is _________ hundredths.

Therefore, 3.69 divided by 3 is ________________

Decide whether you will use grouping or sharing and use the place value chart and counters to solve:

7.55 ÷ 5  8.16 ÷ 3  3.3 ÷ 6

Amir solves 6.39 ÷ 3 using a part whole method.

Use this method to solve

8.48 ÷ 2  6.9 ÷ 3  6.12 ÷ 3
When using the counters to answer $3.27$ divided by $3$, this is what Tommy did:

<table>
<thead>
<tr>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

Tommy says,

I only had 2 counters in the tenths column, so I moved one of the hundredths so each column could be grouped in 3s.

Do you agree with what Tommy has done? Explain why.

Possible answer:

Tommy is incorrect because he cannot move a hundredth to the tenths. He should have exchanged the 2 tenths for hundredths to get an answer of $1.09$.

C is $\frac{1}{4}$ of A

$B = C + 2$

Use the clues to complete the division.

Children may try A as 8 and C as 2 but will realise that this cannot complete the whole division.

Therefore A is 4, B is 3 and C is 1.
Children will apply their understanding of division to solve problems in cases where the answer has up to 2 decimal places.

Children will continue to show division using place value counters and exchanging where needed.

How can we represent this problem using a bar model?

How will we calculate what this item costs?

How will we use division to solve this?

How will we label our bar model to represent this?

Mrs Forbes has saved £4,960. She shares the money between her 15 grandchildren. How much do they each receive?

Modelling clay is sold in two different shops. Shop A sells four pots of clay for £7.68. Shop B sells three pots of clay for £5.79. Which shop has the better deal? Explain your answer.

A box of chocolates costs 4 times as much as a chocolate bar. Together they cost £7.55. How much does each item cost? How much more does the box of chocolates cost?
Each division sentence can be completed using the digits below.

1.3 ÷ 5 = 0.26
12.6 ÷ 3 = 4.2
4.28 ÷ 4 = 1.07

Jack and Rosie are both calculating the answer to 147 ÷ 4

Jack says,
Rosie says,

They are both correct.
Rosie has divided her remainder of 3 by 4 to get 0.75 whereas Jack has recorded his as a remainder.

Who do you agree with?
Decimals as Fractions

Notes and Guidance

Children explore the relationship between decimals and fractions. They start with a decimal and use their place value knowledge to help them convert it into a fraction. Children will use their previous knowledge of exchanging between columns, for example, 3 tenths is the same as 30 hundredths. Once children convert from a decimal to a fraction, they simplify the fraction to help to show patterns.

Mathematical Talk

How would you record your answer as a decimal and a fraction? Can you simplify your answer?

How would you convert the tenths to hundredths?

What do you notice about the numbers that can be simplified in the table?

Can you have a unit fraction that is larger than 0.5? Why?

Varied Fluency

What decimal is shaded? Can you write this as a fraction?

| 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 |

Complete the table.

<table>
<thead>
<tr>
<th>Decimal</th>
<th>Fraction in tenths or hundredths</th>
<th>Simplified fraction</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.6</td>
<td>(\frac{6}{10})</td>
<td>(\frac{3}{5})</td>
</tr>
<tr>
<td>0.1</td>
<td>(\frac{1}{10})</td>
<td></td>
</tr>
<tr>
<td>0.1</td>
<td>(\frac{1}{10})</td>
<td></td>
</tr>
<tr>
<td>0.1</td>
<td>(\frac{1}{10})</td>
<td></td>
</tr>
<tr>
<td>0.95</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Three friends share a pizza. Sam ate 0.25 of the pizza, Mark ate 0.3 of the pizza and Jill ate 0.35 of the pizza.

• Can you write the amount each child ate as a fraction?
• What fraction of the pizza is left?
Decimals as Fractions

Reasoning and Problem Solving

Odd one out.

Possible response:
D is the odd one out because it shows 0.3
Explore how the rest represent 0.6

Alex says,
0.84 is equivalent to \(\frac{84}{10}\)

Possible response:
Alex is wrong because 0.84 is 8 tenths and 4 hundredths and \(\frac{84}{10}\) is 84 tenths.

Which is the odd one out and why?
Notes and Guidance

At this point children should know common fractions, such as thirds, quarters, fifths and eighths, as decimals.

Children explore how finding an equivalent fraction where the denominator is 10, 100 or 1,000 makes it easier to convert from a fraction to a decimal.

They investigate efficient methods to convert fractions to decimals.

Mathematical Talk

How many hundredths are equivalent to one tenth?

How could you convert a fraction to a decimal?

Which is the most efficient method? Why?

Which equivalent fraction would be useful?

Varied Fluency

Match the fractions to the equivalent decimals.

- \( \frac{2}{5} \) = 0.4
- \( \frac{1}{25} \) = 0.04
- \( \frac{1}{4} \) = 0.25

Use your knowledge of known fractions to convert the fractions to decimals. Show your method for each one.

- \( \frac{7}{20} \)
- \( \frac{3}{4} \)
- \( \frac{2}{5} \)
- \( \frac{6}{200} \)

Mo says that \( \frac{63}{100} \) is less than 0.65

Do you agree with Mo?

Explain your answer.
Amir says,

The decimal 0.42 can be read as ‘four tenths and two hundredths’.

Teddy says,

The decimal 0.42 can be read as ‘forty-two hundredths’.

Who do you agree with? Explain your answer.

Both are correct. Four tenths are equivalent to forty hundredths, plus the two hundredths equals forty-two hundredths.

Dora and Whitney are converting \( \frac{30}{500} \) into a decimal.

- Dora doubles the numerator and denominator, then divides by 10
- Whitney divides both the numerator and the denominator by 5
- Both get the answer \( \frac{6}{100} = 0.06 \)

Which method would you use to work out each of the following?

- True because \( \frac{1}{4} \) is 25 hundredths and 0.3 is 30 hundredths. Therefore, 0.3 is bigger.

True or False?

| 0.3 is bigger than \( \frac{1}{4} \) | Explain your reasoning. | 25 \( \frac{500}{500} \) | 125 \( \frac{500}{500} \) | 40 \( \frac{500}{500} \) | 350 \( \frac{500}{500} \) |
| Possible response: | | | | | |

Possible response:

- \( \frac{25}{500} \) - divide by 5, known division fact.
- \( \frac{125}{500} \) - double, easier than dividing 125 by 5
- \( \frac{40}{500} \) - divide by 5, known division fact.
- \( \frac{350}{500} \) - double, easier than dividing 350 by 5
Deena has used place value counters to write $\frac{2}{5}$ as a decimal. She has divided the numerator by the denominator.

Use the short division method to convert the fractions to decimals. Give your answers to 2 decimal places.

In the example provided, we cannot make any equal groups of 5 in the ones column so we have exchanged the 2 ones for 20 tenths. Then we can divide 20 into groups of 5.

8 friends share 7 pizzas. How much pizza does each person get? Give your answer as a decimal and as a fraction.

It is important that children recognise that $\frac{3}{4}$ is the same as $3 ÷ 4$. They can use this understanding to find fractions as decimals by then dividing the numerator by the denominator.

In the example provided, we cannot make any equal groups of 5 in the ones column so we have exchanged the 2 ones for 20 tenths. Then we can divide 20 into groups of 5.

Do we divide the numerator by the denominator or divide the denominator by the numerator? Explain why.

When do we need to exchange?

Are we grouping or are we sharing? Explain why.

Why is it useful to write 2 as 2.0 when dividing by 5?

Why is it not useful to write 5 as 5.0 when dividing by 8?
Reasoning and Problem Solving

Rosie and Tommy have both attempted to convert $\frac{2}{8}$ into a decimal.

Rosie is correct and Tommy is incorrect.

Tommy has divided 8 by 2 rather than 2 divided by 8 to find the answer.

Who is correct? Prove it.

Mo shares 6 bananas between some friends.

Each friend gets 0.75 of a banana.

How many friends does he share the bananas with? Show your method.

Mo shares his 6 bananas between 8 friends because 6 divided by 8 equals 0.75

Children may show different methods:

Method 1: Children add 0.75 until they reach 6. This may involve spotting that 4 lots of 0.75 equals 3 and then they double this to find 8 lots of 0.75 equals 6

Method 2: Children use their knowledge that 0.75 is equivalent to $\frac{3}{4}$ to find the equivalent fraction of $\frac{6}{8}$
Overview

Small Steps

- Understand percentages
- Fractions to percentages
- Equivalent FDP
- Order FDP
- Percentage of an amount (1)
- Percentage of an amount (2)
- Percentages – missing values

Notes for 2020/21

Children should have been introduced to percentages briefly in Y5 but this work may have been missed. Time spent exploring 100 as a denominator, making the link to decimals and hundredths is important. Bar models and hundred squares should be used to support understanding.
Children are introduced to ‘per cent’ for the first time and will understand that ‘per cent’ relates to ‘number of parts per hundred’.

They will explore this through different representations which show different parts of a hundred. Children will use ‘number of parts per hundred’ alongside the % symbol.

Complete the sentence stem for each diagram.

There are ____ parts per hundred shaded. This is ____%

Complete the table.

<table>
<thead>
<tr>
<th>Pictorial</th>
<th>Parts per hundred</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>There are 51 parts per hundred.</td>
<td>75%</td>
</tr>
</tbody>
</table>

Complete the bar models.

If the bar is worth 100%, what is each part worth?
Reasoning and Problem Solving

Oh no! Dexter has spilt ink on his hundred square.

<table>
<thead>
<tr>
<th>Some possible answers:</th>
</tr>
</thead>
<tbody>
<tr>
<td>It could be 25%</td>
</tr>
<tr>
<td>It must be less than 70%</td>
</tr>
<tr>
<td>It can't be 100%</td>
</tr>
</tbody>
</table>

Complete the sentence stems to describe what percentage is shaded.

- It could be...
- It must be...
- It can't be...

Mo, Annie and Tommy all did a test with 100 questions. Tommy got 6 fewer questions correct than Mo.

<table>
<thead>
<tr>
<th>Name</th>
<th>Score</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mo</td>
<td>56 out of 100</td>
<td>56%</td>
</tr>
<tr>
<td>Annie</td>
<td>65%</td>
<td></td>
</tr>
<tr>
<td>Tommy</td>
<td>50%</td>
<td></td>
</tr>
</tbody>
</table>

Complete the table. How many more marks did each child need to score 100%?

Dora and Amir each have 100 sweets. Dora eats 65% of hers. Amir has 35 sweets left.

Who has more sweets left?

- Dora needs 44
- Annie needs 35
- Tommy needs 50

Neither. They both have an equal number of sweets remaining.
It is important that children understand that ‘percent’ means ‘out of 100’.
Children will be familiar with converting some common fractions from their work in Year 5
They learn to convert fractions to equivalent fractions where the denominator is 100 in order to find the percentage equivalent.

What does the word ‘percent’ mean?

How can you convert tenths to hundredths?

Why is it easy to convert fiftieths to hundredths?

What other fractions are easy to convert to percentages?

<table>
<thead>
<tr>
<th>Fraction</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\frac{1}{2}$</td>
<td></td>
</tr>
<tr>
<td>$\frac{1}{4}$</td>
<td></td>
</tr>
<tr>
<td>$\frac{1}{10}$</td>
<td></td>
</tr>
<tr>
<td>$\frac{1}{5}$</td>
<td></td>
</tr>
</tbody>
</table>

Fill in the missing numbers.

$\frac{12}{100} = \square\% \quad \frac{100}{100} = 35\%$

$\frac{12}{50} = \square = \square\% \quad \frac{44}{100} = \square = 22\%$
In a Maths test, Tommy answered 62% of the questions correctly.

Rosie answered $\frac{3}{5}$ of the questions correctly.

Who answered more questions correctly?

Explain your answer.

Tommy answered more questions correctly because $\frac{3}{5}$ as a percentage is 60% and this is less than 62%.

Amir thinks that 18% of the grid has been shaded.

Dora thinks that 36% of the grid has been shaded.

Who do you agree with?

Explain your reasoning.

Dora is correct because $\frac{18}{50} = \frac{36}{100}$.
Equivalent FDP

Notes and Guidance

Children use their knowledge of common equivalent fractions and decimals to find the equivalent percentage.

A common misconception is that 0.1 is equivalent to 1%. Diagrams may be useful to support understanding the difference between tenths and hundredths and their equivalent percentages.

Mathematical Talk

How does converting a decimal to a fraction help us to convert it to a percentage?

How do you convert a percentage to a decimal?

Can you use a hundred square to represent your conversions?

Varied Fluency

Complete the table.

<table>
<thead>
<tr>
<th>Decimal</th>
<th>Fraction</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.35</td>
<td>(\frac{35}{100})</td>
<td>35%</td>
</tr>
<tr>
<td>0.27</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.6</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.06</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Use <, > or = to complete the statements.

0.36 \(\quad\) 40% \(\quad\) \(\frac{7}{10}\) \(\quad\) 0.07

0.4 \(\quad\) 25% \(\quad\) 0.4 \(\quad\) \(\frac{1}{4}\)

Which of these are equivalent to 60%?

\(\frac{60}{100}\) \(\quad\) \(\frac{6}{100}\) \(\quad\) 0.06 \(\quad\) \(\frac{3}{5}\) \(\quad\) \(\frac{3}{50}\) \(\quad\) 0.6
Amir says 0.3 is less than 12% because 3 is less than 12

Amir is wrong because 0.3 is equivalent to 30%

Amir is wrong because 0.3 is equivalent to 30%

Complete the part-whole model. How many different ways can you complete it?

A = 0.3, 30% or $\frac{3}{10}$

B = 0.2, 20%, $\frac{2}{10}$ or $\frac{1}{5}$

C = 0.1, 10% or $\frac{1}{10}$

How many different fractions can you make using the digit cards?

Possible answers:
Children make a range of fractions.
They should be able to convert
$\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{5}$
and $\frac{4}{5}$ into decimals and percentages.
**Order FDP**

**Notes and Guidance**

Children convert between fractions, decimals and percentages to enable them to order and compare them.

Encourage them to convert each number to the same form so that they can be more easily ordered and compared. Once the children have compared the numbers, they will need to put them back into the original form to answer the question.

**Mathematical Talk**

What do you notice about the fractions, decimals or percentages? Can you compare any straight away?

What is the most efficient way to order them?

Do you prefer to convert your numbers to decimals, fractions or percentages? Why?

If you put them in ascending order, what will it look like? If you put them in descending order, what will it look like?

**Varied Fluency**

Use <, > or = to complete the statements:

- 60% __ __ 0.6 __ __ \(\frac{3}{5}\)
- 0.23 __ __ 24% __ __ \(\frac{1}{4}\)
- 37.6% __ __ \(\frac{3}{8}\) __ __ 0.27

Order from smallest to largest:

- 50% __ __ \(\frac{2}{5}\) __ __ 0.45 __ __ \(\frac{3}{10}\) __ __ 54% __ __ 0.05

Four friends share a pizza. Whitney eats 35% of the pizza, Teddy eats 0.4 of the pizza, Dora eats 12.5% of the pizza and Alex eats 0.125 of the pizza.

Write the amount each child eats as a fraction. Who eats the most? Who eats the least? Is there any left?
In his first Geography test, Mo scored 38%.
In the next test he scored \( \frac{16}{40} \) or 40%.
Did Mo improve his score?
Explain your answer.

Mo improved his score.
\( \frac{16}{40} \) is equivalent to 40% which is greater than his previous score of 38%.

Which month did Eva save the most money?
Estimate your answer using your knowledge of fractions, decimals and percentages.

In January, Eva saves \( \frac{3}{5} \) of her £20 pocket money.

In February, she saves 0.4 of her £10 pocket money.

In March, she saves 45% of her £40 pocket money.

She saved the most money in March.
Estimates:
Over £10 in January because \( \frac{3}{5} \) is more than half.
Under £10 in February because she only had £10 to start with and 0.4 is less than half.
Nearly £20 in March because 45% is close to a half.
Percentage of an Amount (1)

Notes and Guidance

Children use known fractional equivalences to find percentages of amounts. Bar models and other visual representations may be useful in supporting this e.g. \(25\% = \frac{1}{4}\) so we divide into 4 equal parts. In this step, we focus on 50%, 25%, 10% and 1% only.

Mathematical Talk

Why do we divide a quantity by 2 in order to find 50%?

How do you calculate 10% of a number mentally?

What’s the same and what’s different about 10% of 300 and 10% of 30?

Varied Fluency

Eva says,

50% is equivalent to \(\frac{1}{2}\)

To find 50% of an amount, I can divide by 2.

Complete the sentences.

25% is equivalent to \(\frac{1}{4}\) To find 25% of an amount, divide by ___

10% is equivalent to \(\frac{1}{10}\) To find 10% of an amount, divide by ___

1% is equivalent to \(\frac{1}{100}\) To find 1% of an amount, divide by ___

Use the bar models to help you complete the calculations.

Find:

50% of 300 = 25% of 300 = 10% of 300 = 1% of 300

50% of 30 = 25% of 30 = 10% of 30 = 1% of 30

50% of 60 = 25% of 60 = 10% of 60 = 1% of 60
### Percentage of an Amount (1)

#### Reasoning and Problem Solving

<table>
<thead>
<tr>
<th>Mo says,</th>
<th>Possible answer:</th>
</tr>
</thead>
<tbody>
<tr>
<td>To find 10% you divide by 10, so to find 50% you divide by 50</td>
<td>Mo is wrong because 50% is equivalent to a half so to find 50% you divide by 2</td>
</tr>
<tr>
<td>Do you agree? Explain why.</td>
<td></td>
</tr>
</tbody>
</table>

- **Eva says** to find 1% of a number, you divide by 100
- **Whitney says** to find 1% of a number, you divide by 10 and then by 10 again.

Who do you agree with? Explain your answer.

<table>
<thead>
<tr>
<th>Complete the missing numbers.</th>
<th>25</th>
</tr>
</thead>
<tbody>
<tr>
<td>50% of 40 = ____% of 80</td>
<td></td>
</tr>
<tr>
<td>____% of 40 = 1% of 400</td>
<td>10</td>
</tr>
<tr>
<td>10% of 500 = ____% of 100</td>
<td>50</td>
</tr>
</tbody>
</table>
Children build on the last step by finding multiples of 10% and other known percentages. They explore different methods of finding certain percentages e.g. Finding 20% by dividing by 10 and multiplying by 2 or by dividing by 5. They also explore finding 5% by finding half of 10%. Using these methods, children build up to find percentages such as 35%.

Is dividing by 10 and multiplying by 5 the most efficient way to find 50%? Explain why.

Is dividing by 10 and multiplying by 9 the most efficient way to find 90%? Explain why.

How many ways can you think of to calculate 60% of a number?

Mo uses a bar model to find 30% of 220

10% of 220 = 22, so 30% of 220 = 3 x 22 = 66

Use Mo’s method to calculate:

40% of 220  20% of 110  30% of 440  90% of 460

To find 5% of a number, divide by 10 and then divide by 2

Use this method to work out:

(a) 5% of 140  (b) 5% of 260  (c) 5% of 1 m 80 cm

How else could we work out 5%?

Calculate:

15% of 60 m  35% of 300 g  65% of £20
Four children in a class were asked to find 20% of an amount, this is what they did:

- **Whitney**: I divided by 5 because 20% is the same as one fifth.
- **Amir**: I found one percent by dividing by 100, then I multiplied my answer by 20.
- **Alex**: I did 10% add 10%.
- **Jack**: I found ten percent by dividing by 10, then I multiplied my answer by 2.

Who do you think has the most efficient method? Explain why. Who do you think will end up getting the answer incorrect?

All methods are acceptable ways of finding 20%. Children may have different answers because they may find different methods easier. Discussion could be had around whether or not their preferred method is always the most efficient.

How many ways can you find 45% of 60? Use similar strategies to find 60% of 45.

What do you notice? Does this always happen? Can you find more examples?

Possible methods include:
- 10% × 4 + 5%
- 25% + 20%
- 25% + 10%+ 10%
- 50% – 5%
- To find 60% of 45
- 10% × 6
- 50% + 10%
- 10% × 3

Children will notice that 45% of 60 = 60% of 45. This always happens.
Children use their understanding of percentages to find the missing whole or a missing percentage when the other values are given. They may find it useful to draw a bar model to help them see the relationship between the given percentage or amount and the whole.

It is important that children see that there may be more than one way to solve a problem and that some methods are more efficient than others.

If we know a percentage, can we work out the whole?

If we know the whole and the amount, can we find what percentage has been calculated?

What diagrams could help you visualise this problem?

Is there more than one way to solve the problem?

What is the most efficient way to find a missing value?

If 7 is 10% of a number, what is the number?

Use the bar model to help you.

Complete:

10% of 150 = 

30% of = 45

30% of 300 = 

30% of = 900

Can you see a link between the questions?
Reasoning and Problem Solving

What percentage questions can you ask about this bar model?

Possible answer:
If 20% of a number is 3.5, what is the whole?
What is 60%?
What is 10%?

Fill in the missing values to make this statement correct.
Can you find more than one way?

Possible answers:
25% of 60 = 75% of 60
25% of 120 = 50% of 60
25% of 24 = 10% of 60
25% of 2.4 = 1% of 60
25% of 180 = 75% of 60

A golf club has 200 members.
58% of the members are male.
50% of the female members are children.

(a) How many male members are in the golf club?
(b) How many female children are in the golf club?

116 male members
42 female children
### Overview

#### Small Steps

<table>
<thead>
<tr>
<th>Topic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Find a rule - one step</td>
</tr>
<tr>
<td>Find a rule - two step</td>
</tr>
<tr>
<td>Forming expressions</td>
</tr>
<tr>
<td>Substitution</td>
</tr>
<tr>
<td>Formulae</td>
</tr>
<tr>
<td>Forming equations</td>
</tr>
<tr>
<td>Solve simple one-step equations</td>
</tr>
<tr>
<td>Solve two-step equations</td>
</tr>
<tr>
<td>Find pairs of values</td>
</tr>
<tr>
<td>Enumerate possibilities</td>
</tr>
</tbody>
</table>

#### Notes for 2020/21

- All of this block is new learning for Year 6 so there are no recap steps.
- Children first look at forming expressions before moving on to solving more complex equations.
- This should be introduced using concrete and pictorial methods alongside the abstract notation.
Find a Rule – One Step

Notes and Guidance

Children explore simple one-step function machines. Explain that a one-step function is where they perform just one operation on the input. Children understand that for each number they put into a function machine, there is an output. They should also be taught to “work backwards” to find the input given the output. Given a set of inputs and outputs, they should be able to work out the function.

Mathematical Talk

What do you think “one-step function” means? What examples of functions do you know? Do some functions have more than one name? What do you think input and output mean? What is the output if ….? What is the input if ....? How many sets of inputs and outputs do you need to be able to work out the function? Explain how you know.

Varied Fluency

Here is a function machine.

\[ \text{Input} \rightarrow \times 4 \rightarrow \text{Output} \]

- What is the output if the input is 2?
- What is the output if the input is 7.2?
- What is the input if the output was 20?
- What is the input if the output was 22?

Complete the table for the function machine.

<table>
<thead>
<tr>
<th>Input</th>
<th>5</th>
<th>5.8</th>
<th>10</th>
<th>(-3)</th>
<th>(-8)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Input</th>
<th>9</th>
<th>169</th>
<th>0</th>
</tr>
</thead>
</table>

Find the missing function.

\[ \begin{array}{c}
10 \rightarrow 5 \\
24 \rightarrow 12 \\
7 \rightarrow 3.5 \\
\end{array} \]
Eva has a one-step function machine. She puts in the number 6 and the number 18 comes out. What could the function be? How many different answers can you find?

The function could be $+12$, $\times3$

Amir puts some numbers into a function machine.

<table>
<thead>
<tr>
<th>Input</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>8</td>
</tr>
<tr>
<td>3</td>
<td>7</td>
</tr>
<tr>
<td>6</td>
<td>4</td>
</tr>
</tbody>
</table>

What is the output from the function when the input is 16?

Dora puts a number into the function machine.

Dora's number is:
- A factor of 32
- A multiple of 8
- A square number

What is Dora's input? What is her output?

Can you create your own clues for the numbers you put into a function machine for a partner to solve?

Dora's input is 16
Her output is 8

Find a Rule – One Step
Find a Rule – Two Step

Notes and Guidance

Children build on their knowledge of one-step functions to look at two-step function machines. Discuss with children whether a function such as + 5 and + 6 is a two-step function machine or whether it can be written as a one-step function. Children look at strategies to find the functions. They can use trial and improvement or consider the pattern of differences. Children record their input and output values in the form of a table.

Mathematical Talk

How can you write + 5 followed by – 2 as a one-step function?
If I change the order of the functions, is the output the same?
What is the output if …?
What is the input if …?
If you add 3 to a number and then add 5 to the result, how much have you added on altogether?

Varied Fluency

Here is a function machine.

- What is the output if the input is 5?
- What is the input if the output is 19?
- What is the output if the input is 3.5?

Complete the table for the given function machine.

<table>
<thead>
<tr>
<th>Input</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- What patterns do you notice in the outputs?
- What is the input if 20 is the output? How did you work it out?

How can you write this two-step machine as a one-step machine?

Check your answer by inputting values.
The function machines will give the same answer.

Is Teddy correct?

Is there an input that will give the same output for both machines?

No they do not give the same answer. Encourage children to refer to the order of operations to help them understand why the outputs are different.

Mo has the following function machines.

The first one can be written as $-6$

The second can be written as $\times 4$

The third cannot be written as a single machine.

Find a Rule – Two Step

Reasoning and Problem Solving

Teddy has two function machines.

<table>
<thead>
<tr>
<th>Input</th>
<th>+ 5</th>
<th>× 2</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input</td>
<td>× 2</td>
<td>+ 5</td>
<td>Output</td>
</tr>
</tbody>
</table>

He says,

The function machines will give the same answer.

Mo has the following function machines.

<table>
<thead>
<tr>
<th>Input</th>
<th>+ 2</th>
<th>− 8</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input</td>
<td>× 8</td>
<td>÷ 2</td>
<td>Output</td>
</tr>
<tr>
<td>Input</td>
<td>× 2</td>
<td>− 8</td>
<td>Output</td>
</tr>
</tbody>
</table>

Explain which of these can be written as single function machines.
Children have now met one-step and two-step function machines with numerical inputs. In this step, children use simple algebraic inputs e.g. $y$. Using these inputs in a function machine leads them to forming expressions e.g. $y + 4$. The use of cubes to represent a variable can aid understanding. Children are introduced to conventions that we use when writing algebraic expressions. e.g. $y \times 4$ as $4y$.

### Notes and Guidance

**Varied Fluency**

Mo uses cubes to write expressions for function machines.

- **Input** $\rightarrow + 4 \rightarrow \text{Output}$
- **Input** $\rightarrow \times 4 \rightarrow \text{Output}$

Use Mo’s method to represent the function machines. What is the output for each machine when the input is $a$?

Eva is writing expressions for two-step function machines.

- **Input** $\rightarrow \times 2 \rightarrow + 3 \rightarrow \text{Output}$

Use Eva’s method to write expressions for the function machines.

### Mathematical Talk

What expressions can be formed from this function machine?

What would the function machine look like for this rule/expression?

How can you write $x \times 3 + 6$ differently?

Are $2a + 6$ and $6 + 2a$ the same? Explain your answer.
Reasoning and Problem Solving

Amir inputs $m$ into these function machines.

He says the outputs of the machines will be the same.

Do you agree?

Explain your answer.

No, because $2m + 1$ isn’t the same as $2m + 2$

This function machine gives the same output for every input. For example if the input is 5 then the output is 5 and so on.

What is the missing part of the function?

What other pairs of functions can you think that will do the same?

Other pairs of functions that will do the same are functions that are the inverse of each other e.g. $+ 3, − 3$
Substitution

Notes and Guidance

Children substitute into simple expressions to find a particular value.

They have already experienced inputting into a function machine, and teachers can make the links between these two concepts.

Children will need to understand that the same expression can have different values depending on what has been substituted.

Mathematical Talk

Which letter represents the star?
Which letter represents the heart?
Would it still be correct if it was written as \( a + b + c \)?

What does it mean when a number is next to a letter?

Is \( a + b + b \) the same as \( a + 2b \)?

Varied Fluency

If \( ⭐ = 7 \) and \( ♡ = 5 \), what is the value of:

\[ ⭐ + ♡ + ♡ \]

If \( a = 7 \) and \( b = 5 \) what is the value of:

\[ a + b + b \]

What is the same and what is different about this question?

Substitute the following to work out the values of the expressions.

- \( w = 3 \quad x = 5 \quad y = 2.5 \)
- \( w + 10 \)
- \( w + x \)
- \( y - w \)
- \( 3y \)
- \( 12 + 8.8w \)
- \( wx \)
- \( wy + 4x \)
Here are two formulae.

\[ p = 2a + 5 \]
\[ c = 10 - p \]

Find the value of \( c \) when \( a = 10 \)

\[ c = -15 \]

\[ x = 2c + 6 \]

Whitney says, \( x = 12 \) because \( c \) must be equal to 3 because it’s the 3rd letter in the alphabet.

Is Whitney correct?

Amir says,

When \( c = 5 \), \( x = 31 \)

Amir is wrong.

What would the correct value of \( x \) be?

No Whitney is incorrect. \( c \) could have any value.

Amir has put the 2 next to the 5 to make 25 instead of multiplying 2 by 5.

The correct value of \( x \) would be 16.
Notes and Guidance

Children substitute into familiar formulae such as those for area and volume.

They also use simple formulae to work out values of everyday activities such as the cost of a taxi or the amount of medicine to take given a person's age.

Mathematical Talk

What tells you something is a formula?

Which of the rectangles is the odd one out? Why?

Could you write the formula for a rectangle in a different way?

What other formulae do you know?

Varied Fluency

Which of the following is a formula?

- \( P = 2l + 2w \)
- \( 3d + 5 \)
- \( 20 = 3x - 2 \)

Explain why the other two are not formulae.

Eva uses the formula \( P = 2l + 2w \) to find the perimeter of rectangles. Use this formula to find the perimeter of rectangles with the following lengths and widths.

- \( l = 15, w = 4 \)
- \( l = 1 \frac{1}{4}, w = 3 \frac{3}{8} \)
- \( l = w = 5.1 \)

This is the formula to work out the cost of a taxi.

\[ C = 1.50 + 0.3m \]

\( C \) = the cost of the journey in £
\( m \) = number of miles travelled.
Work out the cost of a 12-mile taxi journey.
Jack and Dora are using the following formula to work out what they should charge for four hours of cleaning.

Cost in pounds = 20 + 10 × number of hours

Jack thinks they should charge £60
Dora thinks they should charge £120

Who do you agree with? Why?

Jack is correct as multiplication should be performed first following the order of operations.

Dora has not used the order of operations – she has added 20 and 10 and then multiplied 30 by 4

The rule for making scones is use 4 times as much flour ($f$) as butter ($b$).

Which is the correct formula to represent this?

- **A**: $f = \frac{b}{4}$
- **B**: $f = 4b$
- **C**: $f = b + 4$
- **D**: $4f = b$

Explain why the others are incorrect.

B is correct.

A shows the amount of flour is a quarter of the amount of butter.

C shows the amount of flour is 4 more than butter.

D shows butter is 4 times the amount of flour.
### Mathematical Talk

**What does the cube represent?**

**What do the counters represent?**

**Design your own ‘think of a number’ problems.**

**What’s the difference between an expression and an equation?**

**What’s the difference between a formula and an equation?**

### Forming Equations

Building on the earlier step of forming expressions, children now use algebraic notation to form one-step equations. They need to know the difference between an expression like \( x + 5 \), which can take different values depending on the value of \( x \), and an equation like \( x + 5 = 11.2 \) where \( x \) is a specific unknown value. This is best introduced using concrete materials e.g. cubes, can be used to represent the unknown values with counters being used to represent known numbers.

### Varied Fluency

**Amir represents a word problem using cubes, counters and algebra.**

<table>
<thead>
<tr>
<th>Words</th>
<th>Concrete</th>
<th>Algebra</th>
</tr>
</thead>
<tbody>
<tr>
<td>I think of a number</td>
<td>🎈</td>
<td>( x )</td>
</tr>
<tr>
<td>Add 3</td>
<td>🎈 🎈 🎈</td>
<td>( x + 3 )</td>
</tr>
<tr>
<td>My answer is 5</td>
<td>🎈 🎈 🎈 = 🎈 🎈 🎈 🎈 🎈</td>
<td>( x + 3 = 5 )</td>
</tr>
</tbody>
</table>

Complete this table using Amir’s method.

<table>
<thead>
<tr>
<th>Words</th>
<th>Concrete</th>
</tr>
</thead>
<tbody>
<tr>
<td>I think of a number</td>
<td>🎈</td>
</tr>
<tr>
<td>Add 1</td>
<td>🎈 🎈 🎈</td>
</tr>
<tr>
<td>My answer is 8</td>
<td>🎈 🎈 🎈 🎈 = 🎈 🎈 🎈 🎈 🎈 🎈 🎈 🎈</td>
</tr>
</tbody>
</table>

**A book costs £5 and a magazine costs £\( n \)**

The total cost of the book and magazine is £8

Write this information as an equation.

**Write down algebraic equations for these word problems.**

- I think of a number, subtract 17, my answer is 20
- I think of a number, multiply it by 5, my answer is 45
## Reasoning and Problem Solving

<table>
<thead>
<tr>
<th>Rosie thinks of a number. She adds 7 and divides her answer by 2.</th>
<th>They both think of 11, therefore Teddy’s answer is 29.</th>
<th>Eva spends 92p on yo-yos and sweets.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Teddy thinks of a number. He multiples by 3 and subtracts 4.</td>
<td>Rosie and Teddy think of the same number. Rosie’s answer is 9. What is Teddy’s answer?</td>
<td></td>
</tr>
<tr>
<td>Rosie and Teddy think of the same number again. This time, they both get the same answer.</td>
<td>They think of 3 and the answer they both get is 5.</td>
<td>She buys ( y ) yo-yos costing 11p and ( s ) sweets costing 4p. Can you write an equation to represent what Eva has bought?</td>
</tr>
<tr>
<td>Use trial and improvement to find the number they were thinking of.</td>
<td>Can you write a similar word problem to describe this equation?</td>
<td>How many yo-yos and sweets could Eva have bought?</td>
</tr>
<tr>
<td></td>
<td></td>
<td>She could have bought 1 sweet and 8 yo-yos or 4 yo-yos and 12 sweets.</td>
</tr>
</tbody>
</table>

\[
92 = 11y + 4s
\]

\[
74 = 15t + 2m
\]
Children solve simple one step equations involving the four operations.

Children should explore this through the use of concrete materials such as cubes, counters and cups.

It is recommended that children learn to solve equations using a balancing method using inverse operations.

Can you make some of your own equations using cups and counters for a friend to solve?

Why do you think the equation is set up on a balance? What does the balance represent? How does this help you solve the equation?

What is the same and what is different about each bar model?

**One-step Equations**

**Notes and Guidance**

- How many counters is each cup worth?
  - Write down and solve the equation represented by the diagram.

- Solve the equation represented on the scales.
  - Can you draw a diagram to go with the next step?

- Match each equation to the correct bar model and then solve to find the value of x.

- 
x + 5 = 12
- 3x = 12
- 12 = 3 + x

**Varied Fluency**
The perimeter of the triangle is 216 cm.

Form an equation to show this information.

Solve the equation to find the value of \( x \).

Work out the lengths of the sides of the triangle.

\[
3x + 4x + 5x = 216
\]

\[
12x = 216
\]

\[
x = 18
\]

\[
5 \times 18 = 90
\]

\[
3 \times 18 = 54
\]

\[
4 \times 18 = 72
\]

Hannah is 8 years old

Jack is 13 years old

Grandma is \( x + 12 \) years old.

The sum of their ages is 100

Form and solve an equation to work out how old Grandma is.

\[
8 + 13 + x + 12 = 100
\]

\[
33 + x = 100
\]

\[
x = 77
\]

Grandma is 77 years old.

What is the size of the smallest angle in this isosceles triangle?

\[
8y = 180
\]

\[
y = 22.5
\]

Smallest angle = 45°

Check by working them all out and see if they add to 180°
Two-step Equations

Notes and Guidance

Children progress from solving equations that require one-step to equations that require two steps. Children should think of each equation as a balance and solve it through doing the same thing to each side of the equation. This should be introduced using concrete and pictorial methods alongside the abstract notation as shown. Only when secure in their understanding should children try this without the support of bar models or similar representations.

Mathematical Talk

Why do you have to do the same to each side of the equation?

Why subtract 1? What does this do to the left hand side of the equation?

Does the order the equation is written in matter?

What’s the same and what’s different about solving the equations $2x + 1 = 17$ and $2x - 1 = 17$?

Varied Fluency

Here is each step of an equation represented with concrete resources.

$$\begin{align*}
2x + 1 &= 5 \\
-1 &= -1 \\
2x &= 4 \\
\div 2 &= \div 2 \\
x &= 2
\end{align*}$$

Use this method to solve:

$$\begin{align*}
4y + 2 &= 6 \\
9 &= 2x + 5 \\
1 + 5a &= 16
\end{align*}$$

Here is each step of an equation represented by a bar model. Write the algebraic steps that show the solution of the equation.

Use bar models to solve these equations.

$$\begin{align*}
x + x &= 5 \\
12 &= 2x \\
7 &= x
\end{align*}$$

$$\begin{align*}
3b + 4 &= 19 \\
20 &= 4b + 2
\end{align*}$$
Two-step Equations

Reasoning and Problem Solving

The length of a rectangle is $2x + 3$
The width of the same rectangle is $x - 2$
The perimeter is 17 cm.

Find the area of the rectangle.

Alex has some algebra expression cards.

The mean of the cards is 19
Work out the value of each card.

Here is the quadrilateral ABCD.

Here is the quadrilateral ABCD.

The perimeter of the quadrilateral is 80 cm.

AB is the same length as BC.
Find the length of CD.

The mean of the cards is 19

Work out the value of each card.

Card values:
13
18
26

$6x + 2 = 17$
$6x = 15$
$x = 2.5$
Length = 8 cm
Width = 0.5 cm
Area = 4 cm²

$6y + 3 = 57$
$6y = 54$
$y = 9$

$4y + 1 = 21$
$4y = 20$
y = 5

AB = 21 cm
BC = 21 cm
AD = 26 cm
CD = 80 – (21 + 21 + 26) = 12 cm
**Find Pairs of Values (1)**

**Mathematical Talk**

Can \( a \) and \( b \) be the same value?

Is it possible for \( a \) or \( b \) to be zero?

How many possible integer answers are there? Convince me you have them all.

What do you notice about the values of \( c \) and \( d \)?

**Notes and Guidance**

Children use their understanding of substitution to consider what possible values a pair of variables can take.

At this stage we should focus on integer values, but other solutions could be a point for discussion.

Children can find values by trial and improvement, but should be encouraged to work systematically.

**Varied Fluency**

\( a \) and \( b \) are variables:

\[ a + b = 6 \]

There are lots of possible solutions to this equation. Find 5 different possible integer values for \( a \) and \( b \).

\( X \) and \( Y \) are whole numbers.

- \( X \) is a one digit odd number.
- \( Y \) is a two digit even number.
- \( X + Y = 25 \)

Find all the possible pairs of numbers that satisfy the equation.

\( c \times d = 48 \)

What are the possible integer values of \( c \) and \( d \)? How many different pairs of values can you find?
**Reasoning and Problem Solving**

$a$, $b$ and $c$ are integers between 0 and 5

\[
a + b = 6
\]

\[
b + c = 4
\]

Find the values of $a$, $b$ and $c$

How many different possibilities can you find?

Possible answers:

- $a = 4$, $b = 2$, $c = 2$
- $a = 3$, $b = 3$, $c = 1$
- $a = 2$, $b = 4$, $c = 0$

$x$ and $y$ are both positive whole numbers.

Possible answer:

Dora says, $\frac{x}{y} = 4$

Jack says, $x$ will always be a multiple of 4

Dora is correct as $x$ will always have to divide into 4 equal parts e.g. $32 \div 8 = 4$, $16 \div 4 = 4$

Jack is incorrect. $40 \div 10 = 4$ and 10 is not a factor of 4

Explain your answer.
Mathematical Talk

What does $2a$ mean? (2 multiplied by an unknown number)

What is the greatest/smallest number ‘$a$’ can be?

What strategy did you use to find the value of ‘$b$’?

Can you draw a bar model to represent the following equations:

- $3f + g = 20$
- $7a + 3b = 40$

What could the letters represent?

Find Pairs of Values (2)

Notes and Guidance

Building on from the last step, children find possible solutions to equations which involve multiples of one or more unknown.

They should be encouraged to try one number for one of the variables first and then work out the corresponding value of the other variable. Children should then work systematically to test if there are other possible solutions that meet the given conditions.

Varied Fluency

In this equation, $a$ and $b$ are both whole numbers which are less than 12.

$2a = b$

Write the calculations that would show all the possible values for $a$ and $b$.

Chose values of $x$ and use the equation to work out the values of $y$.

$7x + 4 = y$

Can you draw a bar model to represent the following equations:

$2g + w = 15$

$g$ and $w$ are positive whole numbers.

Write down all the possible values for $g$ and $w$, show each of them in a bar model.
Reasoning and Problem Solving

Find Pairs of Values (2)

\( ab + b = 18 \)

Mo says,

Is Mo correct? Explain your answer.

\( a \) and \( b \) must both be odd numbers

Possible answer:

Mo is incorrect. Children may give examples to prove Mo is correct e.g. if \( a = 5 \) and \( b = 3 \), but there are also examples to show he is incorrect e.g. \( a = 2 \) and \( b = 6 \) where \( a \) and \( b \) are both even.

Large beads cost 5p and small beads cost 4p

Rosie has 79p to spend on beads.

How many different combinations of small and large beads can Rosie buy?

Can you write expressions that show all the solutions?

Possible answers:

\[ 3l + 16s \]
\[ 7l + 11s \]
\[ 11l + 6s \]
\[ 15l + s \]
Overview

Small Steps

- Metric measures
- Convert metric measures
- Calculate with metric measures
- Miles and kilometres
- Imperial measures

Notes for 2020/21

All of this block is new learning for Year 6 so there are no recap steps.

Children explore measures in context and build on previous learning about place value.
Choose the unit of measure that would be the most appropriate to measure the items.

- The weight of an elephant
- The volume of water in a bath
- The length of an ant
- The length of a football pitch
- The weight of an apple

**Estimate how much juice the glass holds:**

- 250 ml
- 2 litres
- 0.5 litres
- \( \frac{1}{2} \) kg

**Estimate the height of the door frame:**

- 20 mm
- 20 cm
- 20 m
- 2 km
- 2 m
- 0.2 km
Reasoning and Problem Solving

Teddy thinks his chew bar is 13.2 cm long.

Do you agree? Explain why.

Teddy is wrong because he has not lined up the end of his chew bar with zero. It is actually 8.8 cm long.

Ron’s dog is about $\frac{1}{4}$ of the height of the door.
Ron is three times the height of his dog.
Estimate the height of Ron and his dog.

Here is a train timetable showing the times of trains travelling from Halifax to Leeds.

<table>
<thead>
<tr>
<th>Halifax</th>
<th>Leeds</th>
</tr>
</thead>
<tbody>
<tr>
<td>07:33</td>
<td>08:09</td>
</tr>
<tr>
<td>07:49</td>
<td>08:37</td>
</tr>
<tr>
<td>07:52</td>
<td>08:51</td>
</tr>
</tbody>
</table>

An announcement states all trains will arrive $\frac{3}{4}$ of an hour late.
Which train will arrive in Leeds closest to 09:07?

The first train from Halifax, which will now arrive in Leeds at 08:54.
Mathematical Talk

Children will use their skills of multiplying and dividing by 10, 100 and 1,000 when converting between units of length, mass and capacity.
Children will convert in both directions e.g. m to cm and cm to m. Using metre sticks and other scales will support this step. They will need to understand the role of zero as a place holder when performing some calculations, as questions will involve varied numbers of decimal places.

Notes and Guidance

Varied Fluency

There are ___ grams in one kilogram.
There are ___ kilograms in one tonne.
Use these facts to complete the tables.

<table>
<thead>
<tr>
<th>g</th>
<th>kg</th>
<th>kg</th>
<th>tonnes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1,500</td>
<td></td>
<td>1,202</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2.05</td>
<td></td>
<td>4.004</td>
</tr>
<tr>
<td>1,005</td>
<td></td>
<td>125</td>
<td></td>
</tr>
</tbody>
</table>

There are ___ mm in one centimetre.
There are ___ cm in one metre.
There are ___ m in one kilometre.
Use these facts to complete the table.

<table>
<thead>
<tr>
<th>mm</th>
<th>cm</th>
<th>m</th>
<th>km</th>
</tr>
</thead>
<tbody>
<tr>
<td>44,000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>2,780</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>15.5</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1.75</td>
</tr>
</tbody>
</table>
Reasoning and Problem Solving

Mo thinks that 12,000 g is greater than 20 kg because 12,000 > 20

Explain why Mo is wrong.

Put these capacities in order, starting with the smallest.

3 litres = 3,500 ml
0.4 litres
0.035 litres
450 ml
330 ml

A shop sells one-litre bottles of water for 99p each.

300 ml bottles of water are on offer at 8 bottles for £2

Whitney wants to buy 12 litres of water. Find the cheapest way she can do this.

£11.88 to buy 12 one-litre bottles.

12 litres = 40 bottles of size 300 ml.
40 ÷ 8 = 5 so this will cost
5×2 = £10
Whitney should buy 40 bottles of 300 ml.
Calculate with Metric Measures

Notes and Guidance

Children use and apply their conversion skills to solve measurement problems in context.

Teachers should model the use of pictorial representations, such as bar models, to represent the problem and help them decide which operation to use.

Mathematical Talk

A tube of toothpaste holds 75 ml.

How many tubes can be filled using 3 litres of toothpaste?


To bake buns for a party, Ron used these ingredients:

- 600 g caster sugar
- 0.6 kg butter
- 18 eggs (792 g)
- \(\frac{3}{4}\) kg self-raising flour
- 10 g baking powder

What is the total mass of the ingredients? Give your answer in kilograms.
Jack, Alex and Amir jumped a total of 12.69 m in a long jump competition.

Alex jumped exactly 200 cm further than Jack.

Amir jumped exactly 2,000 mm further than Alex.

What distance did they all jump?
Give your answers in metres.

Dora made a stack of her magazines. Each magazine on the pile is 2.5 mm thick. The total height of the stack is 11.5 cm high. How many magazines does she have in her pile?

Jack jumped 2.23 m.
Alex jumped 4.23 m.
Amir jumped 6.23 m.

Each nail weighs 3.85 grams.
There are 24 nails in a packet.

What would be the total mass of 60 packets of nails? Give your answer in kilograms.

How many packets would you need if you wanted \( \frac{1}{2} \) kg of nails?

How many grams of nails would be left over?
Children need to know that 5 miles is approximately equal to 8 km. They should use this fact to find approximate conversions from miles to km and from km to miles.

They should be taught the meaning of the symbol ‘≈’ as “is approximately equal to”.

Give an example of a length you would measure in miles or km.

If we know 5 miles ≈ 8 km, how can we work out 15 miles converted to km?

Can you think of a situation where you may need to convert between miles and kilometres?

Use this fact to complete:
• 15 miles ≈ _______ km
• 30 miles ≈ _______ km
• _______ miles ≈ 160 km

If 10 miles is approximately 16 km, 1 mile is approximately how many kilometres?
• 2 miles ≈ _______ km
• 4 miles ≈ _______ km
• 0.5 miles ≈ _______ km

In the United Kingdom, the maximum speed on a motorway is 70 miles per hour (mph). In France, the maximum speed on a motorway is 130 kilometres per hour (km/h). Which country has the higher speed limit, and by how much? Give your answer in both units.
### Miles and Kilometres

#### Reasoning and Problem Solving

<table>
<thead>
<tr>
<th>Ron and Annie are running a 5 mile race.</th>
<th>Annie has 1 mile left to run, whereas Ron has 1.2 miles left to run. Ron has the furthest left to run.</th>
<th>Mo cycles 45 miles over the course of 3 days.</th>
</tr>
</thead>
<tbody>
<tr>
<td>I have run 6.4 km so far</td>
<td>I have run 3.8 miles so far</td>
<td>On day 1 he cycles 16 km.</td>
</tr>
<tr>
<td>Who has the furthest left to run?</td>
<td></td>
<td>On day 2 he cycles 32 km / 20 miles.</td>
</tr>
<tr>
<td>The distance between Cardiff and London is 240 km.</td>
<td>240 km ≈ 150 miles</td>
<td>On day 3 he cycles 24 km / 15 miles.</td>
</tr>
<tr>
<td>A car is travelling at 60 mph.</td>
<td>150 ÷ 60 = 2 \frac{1}{2} hours</td>
<td></td>
</tr>
<tr>
<td>How long will it take them to get to London from Cardiff?</td>
<td>Or 60 miles ≈ 96 km</td>
<td></td>
</tr>
<tr>
<td></td>
<td>240 ÷ 96 = 2 \frac{1}{2} hours</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Mo cycles 45 miles over the course of 3 days.

On day 1, he cycles 16 km.

On day 2, he cycles 10 miles further than he did on day 1.

How far does he cycle on day 3?

Give your answer in miles and in kilometres.
Notes and Guidance

Children need to know and use the following facts:
- 1 foot is equal to 12 inches
- 1 pound is equal to 16 ounces
- 1 stone is equal to 14 pounds
- 1 gallon is equal to 8 pints
- 1 inch is approximately 2.5 cm

They should use these to perform related conversions, both within imperial measures and between imperial and metric.

Mathematical Talk

Put these in order of size: 1 cm, 1 mm, 1 inch, 1 foot, 1 metre. How do you know?

When do we use imperial measures instead of metric measures?

Why are metric measures easier to convert than imperial measures?

Varied Fluency

Use these facts to complete:
- 2 feet = ___ inches
- ___ feet = 36 inches
- 6 inches ≈ ___ cm
- 4 feet ≈ ___ cm
- 2 lbs = ___ ounces
- ___ lbs = 320 ounces
- 5 stone = ___ lbs
- ___ stones = 154 lbs

- How many gallons are equivalent to 64 pints?
- How many pints are equivalent to 15 gallons?
- How many gallons are equivalent to 2 pints?
### Reasoning and Problem Solving

#### Imperial Measures

Jack is 6 foot 2 inches tall.

Rosie is 162 cm tall.

Who is taller and by how much?

Jack is 185 cm tall, he is 23 cm taller than Rosie.

60 gallons of water are drunk at a sports day.

Each child drank 3 pints.

How many children were at the sports day?

<table>
<thead>
<tr>
<th>60 gallons = 480 pints</th>
</tr>
</thead>
<tbody>
<tr>
<td>480 ÷ 3 = 160 children</td>
</tr>
</tbody>
</table>

Eva wants to make a cake.

Here are some of the ingredients she needs:
- 8 ounces of caster sugar
- 6 ounces of self-raising flour
- 6 ounces of butter

This is what Eva has in her cupboards:
- 0.5 lbs of caster sugar
- 0.25 lbs of self-raising flour
- \( \frac{3}{8} \) lbs of butter

Does Eva have enough ingredients to bake the cake?
If not, how much more does she need to buy?

Eva has the exact amount of butter and caster sugar, but does not have enough self-raising flour – she needs another 2 ounces.
Overview

Small Steps

- Shapes – same area
- Area and perimeter
- Area of a triangle (1)
- Area of a triangle (2)
- Area of a triangle (3)
- Area of parallelogram
- What is volume?
- Volume – counting cubes
- Volume of a cuboid

Notes for 2020/21

Much of this block is new learning where children build on their knowledge of area and perimeter to explore the area of triangles and parallelograms.

The recap step on volume covers the difference between volume and capacity and gives time to explore the conservation of volume using centimetre cubes.
Children will find and draw rectilinear shapes that have the same area.

Children will use their knowledge of factors to draw rectangles with different areas. They will make connections between side lengths and factors.

What do we need to know in order to work out the area of a shape?

Why is it useful to know your times-tables when calculating area?

Can you have a square with an area of 48 cm²? Why?

How can factors help us draw rectangles with a specific area?

### Mathematical Talk

**Varied Fluency**

Sort the shapes into the Carroll diagram.

<table>
<thead>
<tr>
<th>Quadrilateral</th>
<th>Not a quadrilateral</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area of 12 cm²</td>
<td></td>
</tr>
<tr>
<td>Area of 16 cm²</td>
<td></td>
</tr>
</tbody>
</table>

Now draw another shape in each section of the diagram.

How many rectangles can you draw with an area of 24 cm² where the side lengths are integers?

What do you notice about the side lengths?

Using integer side lengths, draw as many rectangles as possible that give the following areas:

- 17 cm²
- 25 cm²
- 32 cm²
Rosie and Dexter are drawing shapes with an area of 30cm².

Dexter’s shape:
60 cm × 0.5 cm = 30 cm²

Rosie’s shape:
2 cm × 10 cm = 20 cm²
5 cm × 2 cm = 10 cm²
20 cm² + 10 cm² = 30 cm²

Could be split differently.

Both are correct.

Three children are given the same rectilinear shape to draw.

Amir says, “The smallest length is 2 cm.”
Alex says, “The area is less than 30 cm².”
Annie says, “The perimeter is 22 cm.”

What could the shape be?

How many possibilities can you find?

Always, Sometimes, Never?

If the area of a rectangle is odd then all of the lengths are odd.

Children can use squared paper to explore. Possible answers:

Sometimes – 15 cm² could be 5 cm and 3 cm or 60 cm and 0.25 cm
Children should calculate area and perimeter of rectilinear shapes. They must have the conceptual understanding of the formula for area by linking this to counting squares. Writing and using the formulae for area and perimeter is a good opportunity to link back to the algebra block.

Children explore that shapes with the same area can have the same or different perimeters.

### Mathematical Talk

What is the difference between the area and perimeter of a shape?

How do we work out the area and perimeter of shapes? Can you show this as a formula?

Can you have 2 rectangles with an area of 24 cm² but different perimeters?

### Notes and Guidance

Look at the shapes below.

- Do any of the shapes have the same area?
- Do any of the shapes have the same perimeter?

Work out the missing values.

- Draw two rectilinear shapes that have an area of 36 cm² but have different perimeters.
- What is the perimeter of each shape?
True or false?

Two rectangles with the same perimeter can have different areas.

Explain your answer.

A farmer has 60 metres of perimeter fencing.

For every 1 m² he can keep 1 chicken.

How can he arrange his fence so that the enclosed area gives him the greatest area?

---

True. Children explore this by drawing rectangles and comparing both area and perimeter.

The greatest area is a 15 m × 15 m square, giving 225 m².

Children may create rectangles by increasing one side by 1 unit and decreasing one side by 1 unit e.g.

16 × 14 = 224 m²
17 × 13 = 221 m²

Tommy has a 8 cm × 2 cm rectangle. He increases the length and width by 1 cm.

<table>
<thead>
<tr>
<th>Length</th>
<th>Width</th>
<th>Area</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>3</td>
<td></td>
</tr>
</tbody>
</table>

He repeats with a 4 cm × 6 cm rectangle.

<table>
<thead>
<tr>
<th>Length</th>
<th>Width</th>
<th>Area</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>6</td>
<td></td>
</tr>
</tbody>
</table>

What do you notice happens to the areas?

Can you find any other examples that follow this pattern?

Are there any examples that do not follow the pattern?

If the sum of the length and width is 10, then the area will always increase by 11.

Children may use arrays to explore this:

The red and green will always total 10 and the yellow will increase that by 1 to 11.
Area of a Triangle (1)

Notes and Guidance

Children will use their previous knowledge of approximating and estimating to work out the area of different triangles by counting.
Children will need to physically annotate to avoid repetition when counting the squares.
Children will begin to see the link between the area of a triangle and the area of a rectangle or square.

Mathematical Talk

How many whole squares can you see?
How many part squares can you see?
What could we do with the parts?
What does estimate mean?
Why is your answer to this question an estimate of the area?
Revisit the idea that a square is a rectangle when generalising how to calculate the area of a triangle.
## Area of a Triangle (1)

### Reasoning and Problem Solving

<table>
<thead>
<tr>
<th>Mo says the area of this triangle is 15cm²</th>
<th>Mo is incorrect because he has counted the half squares as whole squares.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Is Mo correct? If not, explain his mistake.</td>
<td>9 cm²</td>
</tr>
<tr>
<td>Part of a triangle has been covered. Estimate the area of the whole triangle.</td>
<td>What is the same about these two triangles? What is different?</td>
</tr>
<tr>
<td></td>
<td>Can you create a different right angled triangle with the same area?</td>
</tr>
</tbody>
</table>

Both triangles have an area of 15 cm²
The triangle on the left is a right angled triangle and the triangle on the right is an isosceles triangle.

Children could draw a triangle with a height of 10 cm and a base of 3 cm, or a height of 15 cm and a base of 2 cm.
Area of a Triangle (2)

Notes and Guidance

Children use their knowledge of finding the area of a rectangle to find the area of a right-angled triangle. They see that a right-angled triangle with the same length and perpendicular height as a rectangle will have an area half the size. Using the link between the area of a rectangle and a triangle, children will learn and use the formula to calculate the area of a triangle.

Mathematical Talk

What is the same/different about the rectangle and triangle?

What is the relationship between the area of a rectangle and the area of a right-angled triangle?

What is the formula for working out the area of a rectangle or square?

How can you use this formula to work out the area of a right-angled triangle?

Varied Fluency

Estimate the area of the triangle by counting the squares.

Make the triangle into a rectangle with the same height and width. Calculate the area.

The area of the triangle is ________ the area of the rectangle.

If \( l \) represents length and \( h \) represents height:

\[
\text{Area of a rectangle} = l \times h
\]

Use this to calculate the area of the rectangle.

What do you need to do to your answer to work out the area of the triangle?

Therefore, what is the formula for the area of a triangle?

Calculate the area of these triangles.
Annie is calculating the area of a right-angled triangle.

Do you agree with Annie? Explain your answer.

I only need to know the length of any two sides to calculate the area of a triangle.

Annie is incorrect as it is not sufficient to know any two sides; she needs the base and perpendicular height. Children could draw examples and non-examples.

Possible answers:
- Height: 18 cm Base: 6 cm
- Height: 27 cm Base: 4 cm
- Height: 12 cm Base: 9 cm

What could the length and the height of the triangle be?

How many different integer possibilities can you find?

Calculate the area of the shaded triangle.

Mo says,

I got an answer of 72 cm²

Do you agree with Mo? If not, can you spot his mistake?

The area of the shaded triangle is 24 cm²

Mo is incorrect as he has just multiplied the two numbers given and divided by 2, he hasn’t identified the correct base of the triangle.
Area of a Triangle (3)

Notes and Guidance

Children will extend their knowledge of working out the area of a right-angled triangle to work out the area of any triangle.

They use the formula, base \( \times \) perpendicular height \( \div 2 \) to calculate the area of a variety of triangles where different side lengths are given and where more than one triangle make up a shape.

Mathematical Talk

What does the word perpendicular mean?

What do we mean by perpendicular height?

What formula can you use to calculate the area of a triangle?

If there is more than one triangle making up a shape, how can we use the formula to find the area of the whole shape?

How do we know which length tells us the perpendicular height of the triangle?

Varied Fluency

To calculate the height of a triangle, you can use the formula:

\[
\text{base} \times \text{height} \div 2
\]

Choose the correct calculation to find the area of the triangle.

- \( 10 \times 5 \div 2 \)
- \( 10 \times 4 \div 2 \)
- \( 5 \times 4 \div 2 \)

Estimate the area of the triangle by counting squares.

Now calculate the area of the triangle. Compare your answers.

Calculate the area of each shape.
Class 6 are calculating the area of this triangle.

Here are some of their methods.

- $4 \times 8 \times 16 \div 2$  
- $4 \times 8 \div 2$
- $16 \div 2$  
- $16 \times 4 \div 2$
- $16 \times 8 \div 2$  
- $8 \times 1$

Tick the correct methods.

The correct methods are:

- $16 \times 2 \div 2$
- $4 \times 8 \div 2$

All mistakes are due to not choosing a pair of lengths that are perpendicular.

Children could explore other methods to get to the correct answer e.g. halving the base first and calculating $8 \times 2$ etc.

The shape is made of three identical triangles.

What is the area of the shape?

Each triangle is 6 cm by 11 cm so area of one triangle is $33 \text{ cm}^2$

Total area = $99 \text{ cm}^2$
Area of a Parallelogram

Notes and Guidance

Children use their knowledge of finding the area of a rectangle to find the area of a parallelogram.

Children investigate the link between the area of a rectangle and parallelogram by cutting a parallelogram so that it can be rearranged into a rectangle. This will help them understand why the formula to find the area of parallelograms works.

Mathematical Talk

Describe a parallelogram.

What do you notice about the area of a rectangle and a parallelogram?

What formula can you use to work out the area of a parallelogram?

Varied Fluency

Approximate the area of the parallelogram by counting squares.
Now cut along the dotted line.
Can you move the triangle to make a rectangle?
Calculate the area of the rectangle.

Here are two quadrilaterals.

• What is the same about the quadrilaterals?
• What’s different?
• What is the area of each quadrilateral?

Use the formula base × perpendicular height to calculate the area of the parallelograms.

Area of a Parallelogram

Year 6 | Spring Term | Week 8 to 9 – Measurement: Perimeter, Area & Volume
Teddy has drawn a parallelogram.
The area is greater than 44 m² but less than 48 m².
What could the base length and the perpendicular height of Teddy’s parallelogram be?

Possible answers:
- 9 m by 5 m = 45 m²
- 6.5 m by 7 m = 45.5 m²
- 11 m by 4.2 m = 46.2 m²

Dexter thinks the area of the parallelogram is 84 cm².
What mistake has Dexter made?
What is the correct area?

Dexter has multiplied 14 by 6 when he should have multiplied by 4 because 4 is the perpendicular height of the parallelogram.
The correct area is 56 cm².

Dora and Eva are creating a mosaic.
They are filling a sheet of paper this size.

Dora is using tiles that are rectangular.
Eva’s tiles are parallelograms.

Dora thinks that she will use fewer tiles than Eva to fill the page because her tiles are bigger.
Do you agree? Explain your answer.

Dora is wrong because both hers and Eva’s tiles have the same area and so the same number of tiles will be needed to complete the mosaic.
The area of the paper is 285 cm² and the area of each tile is 15 cm² so 19 tiles are needed to complete the pattern.
What is Volume?

Notes and Guidance

Children understand that volume is the amount of solid space something takes up. They look at how volume is different to capacity, as capacity is related to the amount a container can hold. Children could use centimetre cubes to make solid shapes. Through this, they recognise the conservation of volume by building different solids using the same amount of centimetre cubes.

Mathematical Talk

Does your shape always have 4 centimetre cubes? Do they take up the same amount of space? How can this help us understand what volume is?

If the solid shapes are made up of 1 cm cubes, can you complete the table?

Look at shape A, B and C. What’s the same and what’s different?

How is capacity different to volume?

Varied Fluency

- Take 4 cubes of length 1 cm. How many different solids can you make? What’s the same? What’s different?

- Make these shapes.

- Complete the table to describe your shapes.

<table>
<thead>
<tr>
<th>Shape</th>
<th>Width (cm)</th>
<th>Height (cm)</th>
<th>Length (cm)</th>
<th>Volume (cm³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>B</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>C</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- Compare the capacity and the volume. Use the sentence stems to help you.

Container ___ has a capacity of ____ ml
The volume of water in container ___ is ___ cm³
How many possible ways can you make a cuboid that has a volume of 12cm³?

Possible solutions:

My shape is made up of 10 centimetre cubes.

The height and length are the same size.

What could my shape look like?

Create your own shape and write some clues for a partner.

Possible solutions include:
Volume – Counting Cubes

Notes and Guidance

Children should understand that volume is the space occupied by a 3-D object.

Children will start by counting cubic units (1 cm³) to find the volume of 3D shapes. They will then use cubes to build their own models and describe the volume of the models they make.

Mathematical Talk

What’s the same and what’s different between area and volume?

Can you explain how you worked out the volume? What did you visualise?

What units of measure could we use for volume? (Explore cm³, m³, mm³ etc.)

Varied Fluency

If each cube has a volume of 1 cm³, find the volume of each solid.

Make each shape using multilink cubes.

If each cube has a volume of 1 cm³, what is the volume of each shape?
Place the shapes in ascending order based on their volume. What about if each cube represented 1 mm³, how would this affect your answer? What about if they were 1 m³?

If one multilink cube represents 1 cubic unit, how many different models can you make with a volume of 12 cubic units?
Amir says he will need 8 cm³ to build this shape.

Dora says she will need 10 cm³.

Who do you agree with?

Explain why.

Amir is incorrect because he has missed the 2 cubes that cannot be seen.

Dora is correct because there are 8 cm³ making the visible shape, then there are an additional 2 cm³ behind.

Tommy is making cubes using multilink. He has 64 multilink cubes altogether.

How many different sized cubes could he make?

He says, If I use all of my multilink to make 8 larger cubes, then each of these will be 2 by 2 by 2.

How many other combinations can Tommy make where he uses all the cubes?

Tommy could make:
- 1 × 1 × 1
- 2 × 2 × 2
- 3 × 3 × 3
- 4 × 4 × 4

Possible answers:
- 64 cubes that are 1 × 1 × 1
- 2 cubes that are 3 × 3 × 3; 1 cube that is 2 × 2 × 2;
- 2 cubes that are 1 × 1 × 1
Volume of a Cuboid

Notes and Guidance

Children make the link between counting cubes and the formula \(l \times w \times h\) for calculating the volume of cuboids.

They realise that the formula is the same as calculating the area of the base and multiplying this by the height.

Mathematical Talk

Can you identify the length, width and height of the cuboid?

If the length of a cuboid is 5 cm and the volume is 100 cm³, what could the width and height of the cuboid be?

What knowledge can I use to help me calculate the missing lengths?

Varied Fluency

Complete the sentences for each cuboid.

The length is: __________
The width is: ___________
The height is: __________

The area of the base is: _____ × _____ = _____

Volume = The area of the base × _____ = _____

Calculate the volume of a cube with side length:

4 cm 2 m 160 mm

Use appropriate units for your answers.

The volume of the cuboid is 32 cm³.

Calculate the height.

You might want to use multilink cubes to help you.
Reasoning and Problem Solving

Rosie says,
You can’t calculate the volume of the cube because you don’t know the width or the height.

Do you agree?
Explain why.

You don’t need the rest of the measurements because it’s a cube and all the edges of a cube are equal. Therefore, the width would be 2 cm and the height would be 2 cm.

The volume of the cube is 8 cm³.

Calculate the volume of the shape.

How many different ways can you make a cuboid with a volume of 48 cm³?

Possible answers:

24 × 2 × 1
2 × 6 × 4
6 × 8 × 1
Reasoning and Problem Solving

Ratio

Spring - Block 6
Overview

Small Steps

- Using ratio language
- Ratio and fractions
- Introducing the ratio symbol
- Calculating ratio
- Using scale factors
- Calculating scale factors
- Ratio and proportion problems

Notes for 2020/21

All of this block is new learning for Year 6 so there are no recap steps.

Bar models are a key representation in this topic. Children may need some extra input here if they have not used bar models throughout KS2.
Children will understand that a ratio shows the relationship between two values and can describe how one is related to another.

They will start by making simple comparisons between two different quantities. For example, they may compare the number of boys to girls in the class and write statements such as, “For every one girl, there are two boys”.

Mathematical Talk

How would your sentences change if there were 2 more blue flowers?

How would your sentences change if there were 10 more pink flowers?

Can you write a “For every…” sentence for the number of boys and girls in your class?

Varied Fluency

Complete the sentences.

For every two blue flowers there are ____ pink flowers.  
For every blue flower there are ____ pink flowers.

Use cubes to help you complete the sentences.

For every ____ , there are ____
For every 8 , there are ____
For every 1 , there are ____

How many “For every…” sentences can you write to describe these counters?
Reasoning and Problem Solving

Whitney lays tiles in the following pattern

If she has 16 red tiles and 20 yellow tiles remaining, can she continue her pattern without there being any tiles left over?

Possible responses:

- For every two red tiles there are three yellow tiles. If Whitney continues the pattern she will need 16 red tiles and 24 yellow tiles. She cannot continue the pattern without there being tiles left over.
- 20 is not a multiple of 3

True or False?

- For every red cube there are 8 blue cubes.  **False**
- For every 4 blue cubes there is 1 red cube.  **True**
- For every 3 red cubes there would be 12 blue cubes.  **True**
- For every 16 cubes, 4 would be red and 12 would be blue.  **False**
- For every 20 cubes, 4 would be red and 16 would be blue.  **True**
Children often think a ratio $1:2$ is the same as a fraction of $\frac{1}{2}$.
In this step, they use objects and diagrams to compare ratios and fractions.

How many counters are there altogether?

How does this help you work out the fraction?

What does the denominator of the fraction tell you?

How can a bar model help you to show the mints and chocolates?

The ratio of red counters to blue counters is $1:2$

What fraction of the counters is blue? $\frac{1}{2}$ $\frac{1}{3}$ $\frac{2}{3}$

What fraction of the counters is red? $\frac{1}{2}$ $\frac{1}{3}$ $\frac{2}{3}$

This bar model shows the ratio $2:3:4$

What fraction of the bar is pink? $\frac{1}{4}$
What fraction of the bar is yellow? $\frac{3}{4}$
What fraction of the bar is blue? $\frac{1}{4}$

One third of the sweets in a box are mints. The rest are chocolates.
What is the ratio of mints to chocolates in the box?
Ron plants flowers in a flower bed. For every 2 red roses he plants 5 white roses. He says, \(\frac{2}{5}\) of the roses are red. Is Ron correct?

Ron is incorrect because \(\frac{2}{7}\) of the roses are red. He has mistaken a part with the whole.

Which is the odd one out? Explain your answer.

- One part out of three is a different colour.
- The others are one part out of four.

There are some red and green cubes in a bag. \(\frac{2}{5}\) of the cubes are red.

True or False?

- For every 2 red cubes there are 5 green cubes.
- For every 2 red cubes there are 3 green cubes.
- For every 3 green cubes there are 2 red cubes.
- For every 3 green cubes there are 5 red cubes.

Explain your answers.
Children are introduced to the colon notation as the ratio symbol, and continue to link this with the language ‘for every…, there are…’.
They need to read ratios e.g. 3 : 5 as “three to five”.
Children understand that the notation relates to the order of parts. For example, ‘For every 3 bananas there are 2 apples would be the same as 3 : 2 and for every 2 apples there are 3 bananas would be the same as 2 : 3

What does the : symbol mean in the context of ratio?
Why is the order of the numbers important when we write ratios?
How do we write a ratio that compares three quantities?
How do we say the ratio “3 : 7”?

Write down the ratio of:
• Bananas to strawberries
• Blackberries to strawberries
• Strawberries to bananas to blackberries
• Blackberries to strawberries to bananas

The ratio of red to green marbles is 3 : 7
Draw an image to represent the marbles.
What fraction of the marbles are red?
What fraction of the marbles are green?
Tick the correct statements.

- There are two yellow tins for every three red tins.
- There are two red tins for every three yellow tins.
- The ratio of red tins to yellow tins is 2 : 3
- The ratio of yellow tins to red tins is 2 : 3

Explain which statements are incorrect and why.

The first and last statement are correct. The other statements have the ratios the wrong way round.

In a box there are some red, blue and green pens.

The ratio of red pens to green pens is 3 : 5

For every 1 red pen there are two blue pens.

Write down the ratio of red pens to blue pens to green pens.

<table>
<thead>
<tr>
<th></th>
<th>R : G</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 : 5</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>R : B</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 : 2 or 3 : 6</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>R : B : G</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 : 6 : 5</td>
<td></td>
</tr>
</tbody>
</table>
Children build on their knowledge of ratios and begin to calculate ratios. They answer worded questions in the form of ‘for every... there are...’ and need to be able to find both a part and a whole.
They should be encouraged to draw bar models to represent their problems, and clearly label the information they have been given and what they want to calculate.

How can we represent this ratio using a bar model?
What does each part represent? What will each part be worth?
How many parts are there altogether? What is each part worth?
If we know what one part is worth, can we calculate the other parts?

A farmer plants some crops in a field. For every 4 carrots he plants 2 leeks. He plants 48 carrots in total. How many leeks did he plant? How many vegetables did he plant in total?

Jack mixes 2 parts of red paint with 3 parts blue paint to make purple paint. If he uses 12 parts blue paint, how many parts red paint does he use?

Eva has a packet of sweets. For every 3 red sweets there are 5 green sweets. If there are 32 sweets in the packet in total, how many of each colour are there? You can use a bar model to help you.
Teddy has two packets of sweets. In the first packet, for every one strawberry sweet there are two orange sweets. In the second packet, for every three orange sweets there are two strawberry sweets. Each packet contains 15 sweets in total.

Which packet has more strawberry sweets and by how many?

The first packet has 5 strawberry sweets and 10 orange sweets. The second packet has 6 strawberry sweets and 9 orange sweets.

The second packet has 1 more strawberry sweet than the first packet.

Annie is making some necklaces to sell. For every one pink bead, she uses three purple beads. Each necklace has 32 beads in total.

The cost of the string is £2.80. The cost of a pink bead is 72p. The cost of a purple bead is 65p.

How much does it cost to make one necklace?

Each necklace has 8 pink beads and 24 purple beads. The cost of the pink beads is £5.76. The cost of the purple beads is £15.60. The cost of a necklace is £24.16.
Using Scale Factors

Notes and Guidance

In this step, children enlarge shapes to make them 2 or 3 times as big etc. They need to be introduced to the term “scale factor” as the name for this process.

Children should be able to draw 2-D shapes on a grid to a given scale factor and be able to use vocabulary, such as, “Shape A is three times as big as shape B”.

Mathematical Talk

What does enlargement mean?

What does scale factor mean?

Why do we have to double/triple all the sides of each shape?

Have the angles changed size?

Varied Fluency

Copy these rectangles onto squared paper then draw them double the size, triple the size and 5 times as big.

Copy these shapes onto squared paper then draw them twice as big and three times as big.

Enlarge these shapes by:
- Scale factor 2
- Scale factor 3
- Scale factor 4
Reasoning and Problem Solving

Draw a rectangle 3 cm by 4 cm.

Enlarge your rectangle by scale factor 2.

Compare the perimeter, area and angles of your two rectangles.

Here are two equilateral triangles. The blue triangle is three times larger than the green triangle.

The perimeter has doubled, the area is four times as large, the angles have stayed the same.

Jack says:

The purple triangle is green triangle enlarged by scale factor 3

Possible answer I do not agree because Jack has increased the green shape by adding 3 cm to each side, not increasing it by a scale factor of 3

Find the perimeter of both triangles.
Notes and Guidance

Children find scale factors when given similar shapes. They need to be taught that ‘similar’ in mathematics means that one shape is an exact enlargement of the other, not just they have some common properties.

Children use multiplication and division facts to calculate missing information and scale factors.

Mathematical Talk

What does similar mean?

What do you notice about the length/width of each shape?

How would drawing the rectangles help you?

How much larger/smaller is shape A compared to shape B?

What does a scale factor of 2 mean? Can you have a scale factor of 2.5?
A rectangle has a perimeter of 16 cm. An enlargement of this rectangle has a perimeter of 24 cm.

The length of the smaller rectangle is 6 cm.

Draw both rectangles.

<table>
<thead>
<tr>
<th>Always, sometimes, or never true?</th>
<th>Smaller rectangle: length – 6 cm width – 2 cm</th>
<th>Larger rectangle: length – 9 cm width – 3 cm</th>
<th>Scale factor: 1.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>To enlarge a shape you just need to do the same thing to each of the sides.</td>
<td>Sometimes. This only works when we are multiplying or dividing the lengths of the sides. It does not work when adding or subtracting.</td>
<td>Ron says that these three rectangles are similar.</td>
<td>Ron is incorrect. The orange rectangle is an enlargement of the green rectangle with scale factor 3. The red rectangle, however, is not similar to the other two as the side lengths are not in the same ratio.</td>
</tr>
</tbody>
</table>

Ron says that these three rectangles are similar.

Do you agree? Explain your answer.
Children will apply the skills they have learnt in the previous steps to a wide range of problems in different contexts.

They may need support to see that different situations are in fact alternative uses of ratio.

Bar models will again provide valuable pictorial support.

How much of each ingredient is needed to make soup for:
• 3 people
• 9 people
• 1 person

What else could you work out?

Two shops sell the same pens for these prices.

<table>
<thead>
<tr>
<th>Shop</th>
<th>Pens</th>
<th>Price</th>
</tr>
</thead>
<tbody>
<tr>
<td>Safeway</td>
<td>4</td>
<td>£2.88</td>
</tr>
<tr>
<td>K-mart</td>
<td>7</td>
<td>£4.83</td>
</tr>
</tbody>
</table>

Which shop is better value for money?

The mass of strawberries in a smoothie is three times the mass of raspberries in the smoothie. The total mass of the fruit is 840 g. How much of each fruit is needed.

Strawberries | 840 g
Raspberries  |
### Ratio and Proportion Problems

#### Reasoning and Problem Solving

<table>
<thead>
<tr>
<th>Flapjacks</th>
<th>Alex has two packets of sweets.</th>
<th>Second packet: 15 orange 5 strawberry.</th>
</tr>
</thead>
<tbody>
<tr>
<td>120 g butter</td>
<td>In the first packet, for every 2 strawberry sweets there are 3 orange.</td>
<td>So there are 20 sweets in each packet.</td>
</tr>
<tr>
<td>100 g brown sugar</td>
<td>In the second packet, for one strawberry sweet, there are three orange.</td>
<td>First packet: 8 strawberry 12 orange</td>
</tr>
<tr>
<td>4 tablespoons golden syrup</td>
<td>Each packet has the same number of sweets.</td>
<td>The first packet contains 8 strawberry sweets.</td>
</tr>
<tr>
<td>250 g oats</td>
<td>The second packet contains 15 orange sweets.</td>
<td></td>
</tr>
<tr>
<td>40 g sultanas</td>
<td>How many strawberry sweets are in the first packet?</td>
<td></td>
</tr>
</tbody>
</table>

This recipe makes 10 flapjacks.

**Reasoning**

Amir has 180 g butter.

What is the largest number of flapjacks he can make?

How much of the other ingredients will he need?
**Small Steps**

- Read and interpret line graphs
- Draw line graphs
- Use line graphs to solve problems
- Circles
- Read and interpret pie charts
- Pie charts with percentages
- Draw pie charts
- The mean

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**Notes for 2020/21**

Time is limited at this stage in Year 6. Line graphs have been covered extensively in Year 4 and 5 so you may choose to skip these steps or merge them into one lesson. This will leave more time for pie charts and the mean.
Mathematical Talk

Where might you see a line graph used in real life?

Why is the ‘Water Consumption’ graph more difficult to interpret?

How can you make sure that you read the information accurately?

Notes and Guidance

Children will build on their experience of interpreting data in context from Year 5, using their knowledge of scales to read information accurately. Examples of graphs are given but it would be useful if real data from across the curriculum e.g. Science, was also used. Please note that line graphs represent continuous data not discrete data. Children need to read information accurately, including where more than one set of data is on the same graph.

Varied Fluency

What is the same and what is different about the two graphs?

Here is a graph showing daily water consumption over two days.

At what times of the day was the same amount of water consumed on Monday and Tuesday?

Was more water consumed at 2 p.m. on Monday or Tuesday morning? How much more?
Reasoning and Problem Solving

Eva has created a graph to track the growth of a plant in her house.

Eva recorded the following facts about the graph.

a) On the 9th of July the plant was about 9 cm tall.

b) Between the 11th and 19th July the plant grew about 5 cm.

c) At the end of the month the plant was twice as tall as it had been on the 13th. Can you spot and correct Eva’s mistakes?

a) On the 9th July a more accurate measurement would be 7.5 cm.

b) Correct.

c) On the 31st the plant was approximately 28 cm tall, but on the 13th it was only 10 cm which is not half of 28 cm. The plant was closer to 14 cm on the 17th July.

Write a story and 3 questions for each of the 3 graphs below.

Possible context for each story:

a) A car speeding up, travelling at a constant speed, then slowing down.

b) The height above sea level a person is at during a walk.

c) Temperature in an oven when you are cooking something.
Draw Line Graphs

Notes and Guidance

Children will build on their experience of reading and interpreting data in order to draw their own line graphs.

Although example contexts are given, it would be useful if children can see real data from across the curriculum.

Children will need to decide on the most appropriate scales and intervals to use depending on the data they are representing.

Mathematical Talk

What will the x-axis represent? What intervals will you use?

What will the y-axis represent? What intervals will you use?

How will you make it clear which line represents which set of data?

Why is it useful to have both sets of data on one graph?

Varied Fluency

This table shows the height a rocket reached between 0 and 60 seconds.

Create a line graph to represent the information.

The table below shows the population in the UK and Australia from 1990 to 2015.

Create one line graph to represent the population in both countries. Create three questions to ask your friend about your completed graph.

<table>
<thead>
<tr>
<th>Time (seconds)</th>
<th>Height (metres)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>10</td>
<td>8</td>
</tr>
<tr>
<td>20</td>
<td>15</td>
</tr>
<tr>
<td>30</td>
<td>25</td>
</tr>
<tr>
<td>40</td>
<td>37</td>
</tr>
<tr>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>60</td>
<td>70</td>
</tr>
</tbody>
</table>
Reasoning and Problem Solving

This graph shows the distance a car travelled.

Rosie and Jack were asked to complete the graph to show the car had stopped. Here are their completed graphs.

Rosie: [graph showing correct completion]

Jack: [graph showing incorrect completion]

Who has completed the graph correctly? Explain how you know.

Rosie has completed the graph correctly. The car has still travelled 15 miles in total, then stopped for 15 minutes before carrying on.

This table shows the distance a lorry travelled during the day.

<table>
<thead>
<tr>
<th>Time</th>
<th>Distance in miles</th>
</tr>
</thead>
<tbody>
<tr>
<td>7.00 a.m.</td>
<td>10</td>
</tr>
<tr>
<td>8.00 a.m.</td>
<td>28</td>
</tr>
<tr>
<td>9.00 a.m.</td>
<td>42</td>
</tr>
<tr>
<td>10.00 a.m.</td>
<td>58</td>
</tr>
<tr>
<td>11.00 a.m.</td>
<td>70</td>
</tr>
<tr>
<td>12.00 a.m.</td>
<td>95</td>
</tr>
<tr>
<td>1:00 p.m.</td>
<td>95</td>
</tr>
<tr>
<td>2:00 p.m.</td>
<td>118</td>
</tr>
</tbody>
</table>

Create a line graph to represent the information, where the divisions along the x-axis are every two hours. Create a second line graph where the divisions along the x-axis are every hour. Compare your graphs. Which graph is more accurate? Would a graph with divisions at each half hour be even more accurate?

Children may find that the second line graph is easier to draw and interpret as it matches the data given directly.

They may discuss that it would be difficult to draw a line graph showing half hour intervals, as we cannot be sure the distance travelled at each half hour.
Notes and Guidance

Once children can read, interpret and draw lines graphs they need to be able to use line graphs to solve problems.

Children need to use their knowledge of scales to read information accurately. They need to be exposed to graphs that show more than one set of data.

At this point, children should be secure with the terms $x$ and $y$ axis, frequency and data.

Mathematical Talk

What do you notice about the scale on the vertical axis? Why might it be misleading? What other scale could you use?

How is the information organised? Is it clear? What else does this graph tell you? What does it not tell you?

How can you calculate ________? Why would this information be placed on a line graph and not a different type of graph?

Varied Fluency

Ron and Annie watched the same channel, but at different times. The graph shows the number of viewers at different times.

Ron watched ‘Chums’ at 5 p.m. Annie watched ‘Countup’ at 8 p.m.

What was the difference between the number of viewers at the start of each programme? What was the difference in the number of viewers between 6 p.m. and 8 p.m.? Which time had twice as many viewers as 6 p.m.?

Two families were travelling to Bridlington for their holidays. They set off at the same time but arrived at different times.

What time did family A arrive? How many km had each family travelled at 08:45? Which family stopped midway through their journey? How much further had they left to travel?
What could this graph be showing?

Possible response: This graph shows the height of two drones and the time they were in the air.

For example:

The graph below shows some of Mr Woolley’s journeys.

What is the same and what is different about each of these journeys?

What might have happened during the green journey?

Possible responses:

All the journeys were nearly the same length of time.

The journeys were all different distances.

The red and blue journey were travelling at constant speeds but red was travelling quicker than blue.

During the green journey, Mr Woolley might have been stuck in traffic or have stopped for a rest.
Circles

Notes and Guidance

Children will illustrate and name parts of circles, using the words radius, diameter, centre and circumference confidently.

They will also explore the relationship between the radius and the diameter and recognise the diameter is twice the length of the radius.

Mathematical Talk

Why is the centre important?

What is the relationship between the diameter and the radius? If you know one of these, how can you calculate the other?

Can you use the vocabulary of a circle to describe and compare objects in the classroom?

Varied Fluency

Using the labels complete the diagram:

Find the radius or the diameter for each object below:

The radius is ___. The diameter is ___. I know this because ___.

Complete the table:

<table>
<thead>
<tr>
<th>Radius</th>
<th>Diameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>26 cm</td>
<td>37 mm</td>
</tr>
<tr>
<td>2.55 m</td>
<td></td>
</tr>
<tr>
<td>99 cm</td>
<td></td>
</tr>
<tr>
<td>19.36 cm</td>
<td></td>
</tr>
</tbody>
</table>
Alex says:

The bigger the radius of a circle, the bigger the diameter.

Do you agree? Explain your reasoning.

I agree with Alex because the diameter is always twice the length of the radius.

Spot the mistake!
Tommy has measured and labelled the diameter of the circle below. He thinks that the radius of this circle will be 3.5 cm.

Is Tommy right? Explain why.

Tommy has measured the diameter inaccurately because the diameter always goes through the centre of the circle from one point on the circumference to another.

Here are 2 circles. Circle A is blue; Circle B is orange. The diameter of Circle A is \( \frac{3}{4} \) the diameter of Circle B.

If the diameter of Circle B is 12 cm, what is the diameter of Circle A?
If the diameter of Circle A is 12 cm, what is the radius of Circle B?
If the diameter of Circle B is 6 cm, what is the diameter of Circle A?
If the diameter of Circle A is 6 cm, what is the radius of Circle B?

A bar model may support children in working these out e.g.

A: \( \frac{6}{2} \) cm, B: \( \frac{8}{2} \) cm

a) 9 cm
b) 16 cm
c) 4.5 cm
d) 8 cm
Children will build on their understanding of circles to start interpreting pie charts. They will understand how to calculate fractions of amounts to interpret simple pie charts.

Children should understand what the whole of the pie chart represents and use this when solving problems.

Mathematical Talk

What does the whole pie chart represent? What does each colour represent?

Do you recognise any of the fractions? How can you use this to help you?

What's the same and what's different about the favourite drinks pie charts?

What other questions could you ask about the pie chart?

Varied Fluency

There are 600 pupils at Copingham Primary school. Work out how many pupils travel to school by:

a) Train
b) Car
c) Cycling
d) Walking

Classes in Year 2 and Year 5 were asked what their favourite drink was. Here are the results:

What fraction of pupils in Year 5 chose Fizzeraid?
How many children in Year 2 chose Rolla Cola?
How many more children chose Vomto than Rolla Cola in Year 2?
What other questions could you ask?
In a survey people were asked what their favourite season of the year was. The results are shown in the pie chart below. If 48 people voted summer, how many people took part in the survey?

**Reasoning and Problem Solving**

*Explain your method.*

Summer is a quarter of the whole pie chart and there are 4 quarters in a whole, so $48 \times 4 = 184$ people in total.

96 people took part in this survey.

96 people took part in this survey.

Our favourite pets

- Hamsters
- Horses
- Dogs
- Cats

How many people voted for cats?

$\frac{3}{8}$ of the people who voted for dogs were male. How many females voted for dogs?

What other information can you gather from the pie chart?

Write some questions about the pie chart for your partner to solve.
Children will apply their understanding of calculating percentages of amounts to interpret pie charts.

Children know that the whole of the pie chart totals 100%.

Encourage children to recognise fractions in order to read the pie chart more efficiently.

**Notes and Guidance**

**Mathematical Talk**

How did you calculate the percentage? What fraction knowledge did you use?

How else could you find the difference between Chocolate and Mint Chocolate?

If you know 5% of a number, how can you work out the whole number?

If you know what 5% is, what else do you know?

**Varied Fluency**

150 children voted for their favourite ice cream flavours. Here are their results:

- How many people voted for Vanilla?
- How many more people voted for Chocolate than Mint Chocolate Chip?
- How many people chose Chocolate, Banana and Vanilla altogether?

There are 200 pupils in Key Stage 2 who chose their favourite hobbies.

- How many pupils chose each hobby?
Reasoning and Problem Solving

15 people in this survey have no siblings. Use this information to work out how many people took part in the survey altogether.

<table>
<thead>
<tr>
<th>Number of siblings</th>
<th>No siblings</th>
<th>1 sibling</th>
<th>2 siblings</th>
<th>3 siblings</th>
<th>4 siblings</th>
<th>5 siblings</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>15</td>
<td>27</td>
<td>30</td>
<td>51</td>
<td>84</td>
<td>93</td>
<td>300</td>
</tr>
</tbody>
</table>

Now work out how many people each segment of the pie chart is worth.

Can you represent the information in a table?

120 boys and 100 girls were asked which was their favourite subject. Here are the results:

- **Boys Favourite Subjects**
  - Maths: 35% of 120 = 42
  - English: 15% of 120 = 18
  - Science: 50% of 120 = 60

- **Girls Favourite Subjects**
  - Maths: 20% of 100 = 20
  - English: 20% of 100 = 20
  - Science: 50% of 100 = 50

Jack says: More girls prefer Maths than boys because 60% is bigger than 50%.

Do you agree? Explain why.

Jack is incorrect because the same amount of girls and boys like maths.
- Boys: 50% of 120 = 60
- Girls: 60% of 100 = 60
Pupils will build on angles around a point totalling 360 degrees to know that this represents 100% of the data within a pie chart.

From this, they will construct a pie chart, using a protractor to measure the angles. A “standard” protractor has radius 5 cm, so if circles of this radius are drawn, it is easier to construct the angles.

How many degrees are there around a point? How will this help us construct a pie chart?

If the total frequency is _____, how will we work out the number of degrees representing each sector?

If 180° represents 15 pupils. How many people took part in the survey? Explain why.

A survey was conducted to show how children in Class 6 travelled to school.

Draw a pie chart to represent the data.
Reasoning and Problem Solving

A survey was conducted to work out Year 6’s favourite sport. Work out the missing information and then construct a pie chart.

<table>
<thead>
<tr>
<th>Favourite sport</th>
<th>Number of children</th>
<th>Convert to degrees</th>
</tr>
</thead>
<tbody>
<tr>
<td>Football</td>
<td>10</td>
<td>$10 \times 6 = 60^\circ$</td>
</tr>
<tr>
<td>Tennis</td>
<td>18</td>
<td>$18 \times 6 = 108^\circ$</td>
</tr>
<tr>
<td>Rugby</td>
<td></td>
<td>$15 \times 6 = 90^\circ$</td>
</tr>
<tr>
<td>Swimming</td>
<td>6</td>
<td>$6 \times 6 = 36^\circ$</td>
</tr>
<tr>
<td>Cricket</td>
<td>7</td>
<td>$7 \times 6 = 42^\circ$</td>
</tr>
<tr>
<td>Golf</td>
<td>4</td>
<td>$4 \times 6 = 24^\circ$</td>
</tr>
<tr>
<td>Total</td>
<td>60</td>
<td>$360^\circ$</td>
</tr>
</tbody>
</table>

Children will then use this to draw a pie chart.

A restaurant was working out which Sunday dinner was the most popular. Use the data to construct a pie chart.

<table>
<thead>
<tr>
<th>Dinner choice</th>
<th>Frequency</th>
<th>Convert to degrees</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chicken</td>
<td>11</td>
<td>$11 \times 9 = 99^\circ$</td>
</tr>
<tr>
<td>Pork</td>
<td>8</td>
<td>$8 \times 9 = 72^\circ$</td>
</tr>
<tr>
<td>Lamb</td>
<td>6</td>
<td>$6 \times 9 = 54^\circ$</td>
</tr>
<tr>
<td>Beef</td>
<td>9</td>
<td>$9 \times 9 = 81^\circ$</td>
</tr>
<tr>
<td>Vegetarian</td>
<td>6</td>
<td>$6 \times 9 = 54^\circ$</td>
</tr>
<tr>
<td>Total</td>
<td>40</td>
<td>$360^\circ$</td>
</tr>
</tbody>
</table>

Miss Jones is carrying out a survey in class about favourite crisp flavours. 15 pupils chose salt and vinegar.

<table>
<thead>
<tr>
<th></th>
<th>Frequency</th>
<th>Convert to degrees</th>
</tr>
</thead>
<tbody>
<tr>
<td>Salt &amp; Vinegar</td>
<td>180</td>
<td>$180^\circ$</td>
</tr>
<tr>
<td>Prawn Cocktail</td>
<td>72</td>
<td>$72^\circ$</td>
</tr>
<tr>
<td>Cheese &amp; Onion</td>
<td>180</td>
<td>$180^\circ$</td>
</tr>
<tr>
<td>Ready Salted</td>
<td>72</td>
<td>$72^\circ$</td>
</tr>
<tr>
<td>Total</td>
<td>40</td>
<td>$360^\circ$</td>
</tr>
</tbody>
</table>

15 pupils $= 180^\circ$
$180 \div 15 = 12$
$12^\circ = 1$ pupil
$72 \div 12 = 6$
pupils
$15 - 6 = 9$
9 fewer students chose ready salted over salt and vinegar.
The Mean

Notes and Guidance

Children will apply their addition and division skills to calculate the mean average in a variety of contexts. They could find the mean by sharing equally or using the formula:

$$\text{Mean} = \frac{\text{Total}}{\text{number of items}}.$$  

Once children understand how to calculate the mean of a simple set of data, allow children time to investigate missing data when given the mean.

Mathematical Talk

What would the total be? If we know the total, how can we calculate the mean?

Do you think calculating the mean age of the family is a good indicator of their actual age? Why? *(Explore why this isn’t helpful).*

When will the mean be useful in real life?

Varied Fluency

Here is a method to find the mean.

<table>
<thead>
<tr>
<th>No. of glasses of juice drunk by 3 friends</th>
<th>Total glasses of juice drank</th>
<th>If each friend drank the same no. of glasses</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1" alt="Glasses of Juice" /></td>
<td><img src="image2" alt="Glasses of Juice" /></td>
<td><img src="image3" alt="Glasses of Juice" /></td>
</tr>
</tbody>
</table>

The mean number of glasses of juice drunk is 3

Use this method to calculate the mean average for the number of slices of pizza eaten by each child.

<table>
<thead>
<tr>
<th>Crayon colour</th>
<th>Amount</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blue</td>
<td>14</td>
</tr>
<tr>
<td>Green</td>
<td>11</td>
</tr>
<tr>
<td>Red</td>
<td>10</td>
</tr>
<tr>
<td>Yellow</td>
<td>9</td>
</tr>
</tbody>
</table>

Calculate the mean number of crayons:

Hassan is the top batsman for the cricket team. His scores over the year are: 134, 60, 17, 63, 38, 84, 11

Calculate the mean number of runs Hassan scored.
The mean number of goals scored in 6 football matches was 4.
Use this information to calculate how many goals were scored in the 6th match:

<table>
<thead>
<tr>
<th>Match number</th>
<th>Number of goals</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>8</td>
</tr>
<tr>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>3</td>
<td>6</td>
</tr>
<tr>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>5</td>
<td>1</td>
</tr>
<tr>
<td>6</td>
<td>1</td>
</tr>
</tbody>
</table>

Three football teams each play 10 matches over a season. The mean number of goals scored by each team was 2.
How many goals might the teams have scored in each match?
How many solutions can you find?

As the mean is 4, the total must be $6 \times 4 = 24$.
The missing number of goals is 3.

Any sets of 10 numbers that total 20 e.g.
2, 2, 2, 2, 2, 2, 2, 2, 2 and 2
3, 1, 4, 5, 3, 1, 3, 0, 0 and 0 etc.

Work out the age of each member of the family if:
Mum is 48 years old.
Teddy is 4 years older than Jack and 7 years older than Alex.

Mum

Dad

Teddy

Jack

Alex

Eva

Mean age of 50

Mean age of 13

Mean age of 6

Calculate the mean age of the whole family.

Mum 48

Dad 52

Teddy 15

Jack 11

Alex 8

Eva 4

23